A STRUCTURAL MODEL FOR DATABASE SYSTEMS

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ABSTRACT

This report presents a model to be used for database design. Because our motivation extends to providing guidance for the structured implementation of a database, we call our model the Structural Model. We derive the design using criteria of correctness, relevance, and performance from semantic and operational specifications obtained from multiple sources. These sources typically correspond to prospective users or user groups of the database. The integration of such specifications is a central issue in the development of an integrated structural database model.

The structural model is used for the design of the logical structures that represent a real-world situation. However, it is not meant to represent all possible real-world semantics, but a subset of the semantics which are important in database modeling.

The model uses relations as building blocks, and hence can be considered as an extension of Codd's relational model [Codd70]. The main extensions to the relational model are the explicit representation of logical connections between relations, the inclusion of insertion-deletion constraints in the model itself, and the separation of relations into several structural types.

Connections between relations are used to represent existence dependencies of tuples in different relations. These existence dependencies are important for the definition of semantics of relationships between classes of real-world entities. The connections between relations are used to specify these existence dependencies, and to ensure that they remain valid when the database is updated. Hence, connections implicitly define a basic, limited set of integrity constraints on the database, those that identify and maintain existence dependencies among tuples from different relations. Consequently, the rules for the maintenance of the structural integrity of the model under insertion and deletion of tuples are easy to specify.

Structural relation types are used to specify how each relation may be connected to other relations in the model. Relations are classified into five types: primary relations, referenced relations, nest relations, association relations, and lexicon relations. The motivation behind the choice of these relation types is discussed, as is their usage in data model design.

A methodology for combining multiple, overlapping data models — also called user views in the literature — is associated with the structural model. The database model, or conceptual schema, which represents the integrated database, may thus be derived from the individual data models of the users. We believe that the structural model can be used to represent the data relationships within the conceptual schema of the ANSI/SPARC DBMS model since it can support database submodels, also called external schema, and maintain the integrity of the submodels with respect to the integrity constraints expressible in the structural model.

We then briefly discuss the usage of the structural model in database design and implementation. The structural model provides a tool to deal effectively with the complexity of large, real-world databases.

We begin this report with a very short review of existing database models. In Chapter 2, we state the purpose of the model, and in Chapter 3 we describe the structural model, first informally and then using a formal framework based on extensions of the relational model. Chapter 4 defines the representations we use, and Chapter 5 covers the integration of data models that represent the different user specifications into an integrated database model. Formal descriptions and examples of the prevalent cases are given.

The work is then placed into context first relative to other work (Chapter 6) and then briefly within our methodology for database design (Chapter 7).
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1. CURRENT STATE OF DATA MODELS

Database systems have become a major topic of interest because of their widespread use in industry, commerce, government, and educational institutions [Steel74, Sibley76, Fry76]. Several data models have been proposed to represent the structure of databases. The most widely discussed models are the relational model [Codd70], the hierarchical model [Tsichritzis76], and the network model (derived from the CODASYL database system specification [CODASYL74]). The majority of implemented database systems use one of the above models. For an excellent introduction to these three database models, see [CompSurv78].

1.1. The relational model:

The relational model is formed from relations. Each relation is composed of a set of structurally identical tuples. Tuples are composed of related data elements. For each relation, a relation description, or schema, defines the attributes and the possible values for the data elements that each tuple in the relation may take. The sets of tuples in a relation is described using the mathematical theory of relations, augmented with the concept of functional dependency among attributes. The mathematical basis of the relational model, the uniform representation of all structures as relations, and the syntactic clarity of the data model schema provide important advantages for model and query analysis.

The relational model has been subjected to intensive theoretical scrutiny. Third normal form [Codd72], and Boyce-Codd normal form [Codd74] have been defined to design relations with favorable update properties. Bernstein [Bernstein75] describes an algorithm for synthesis of third normal form relations from functional dependencies. Fagin [Fagin77] introduced multivalued dependencies and a fourth normal form for relations to extend the understanding of the logical design of relational databases.

When relations are built solely from the functional or multivalued dependencies among all attributes in the data model, several possible logical data models can be derived [Bernstein75, Fagin77, Chang78, Delobel78]. Further, some of the data models will not have a direct correspondence with the actual real-world situation being modelled [Schmid75]. Then the database designer, or some automatic procedure, has to choose the most suitable model.

A drawback of the basic relational model is that known relationships among entities of the situation being model are not explicitly represented but have to be recognized at query processing time by matching attributes that have the same domain. This requires recognition of similar domains, using the schema, as well as some computation within the database to match data elements. Also, logical integrity constraints are not defined within the model, but are left to be defined by the database implementors. In one approach, integrity constraints are described by assertions [Stonebraker74, Eswaran75].

1.2. The hierarchical model:

The hierarchical model represents classes of entities and hierarchical relationships among different entity classes. A class of entities is represented as a record type, and the hierarchical relationships are represented by a tree structure, with record types as nodes in the tree. The record type represents the attributes of a class of entities, while each record represents a particular entity of the class, and is composed of data items that describe the entity.

Each record is owned by only one record of the record type at the level above it in the tree, and can own in turn any number of records of the record types below it, if any. Many real world situations are naturally hierarchical, and are thus well represented by a hierarchical model. In
particular, individual user views, or data models, are often hierarchical. Databases used by multiple users often need a more complex model. In the hierarchical model, non-hierarchical relationships are represented in an awkward and non-symmetric fashion by defining duplicate record types and using pointers.

1.3. The network model:

The network model allows representation of non-hierarchical relationships among entity classes. A record type may be owned by more than one record type, leading to a network representation of m:n relationships among entity classes. The concept of a link-set between two record types is introduced. A link-set groups together records of one record type, the member record type, that are owned by a particular record of a different record type, the owner record type. Existence dependencies to govern occurrences of owner and member records of a link-set are specified by different types of link-sets, such as manual and automatic.

The database administrator may specify the access structure used for implementing a link-set as a chain of pointers, a pointer array, or he may specify that the records be stored physically adjacent. Thus access to the records in a particular link-set via the owner record can be very efficient. However, the database designer has to recognize and define the link-set and its access structure a priori, and queries based on structures not directly implemented may be quite costly to process.

A drawback of the network model is that only implemented relationships can be exploited, and that, due to implementation constraints, certain relationships are difficult to express (such as recursive sets [Taylor76], which are relationships between records of the same record type). Another criticism is that it is too implementation oriented, and thus provides limited data independence [Engles69].

1.4. Some other data models:

The problems with the relational, hierarchical and network models have led to active research in data models. Chang [Chang78] has developed an approach with a ‘database skeleton’ which includes semantic information about the relationships between database relations, and defines the relationships over a time frame using the concept of the “state” of the database. The semantic information is used by the system in query translation, and incomplete or “fuzzy” queries may be processed. Manacher [Manacher75] differentiates relationships into several semantic categories. Abrial [Abrial74] goes further by distinguishing every relationship according to its particular semantic notion, but states that his model would be too complicated for database construction.

Chen [Chen78] has proposed a model based on the relational model which clearly distinguishes relations into two types: entities and relationships among the entities. Integrity rules for logical consistency are considered for the relation types, but are not part of the model. Schmid and Swenson [Schmid75] develop the semantics of the relational model, and show that, in the context of their model, relations in third normal form can be differentiated into five semantic types. Rules for insertion and deletion of tuples are given.

More recently, models have been introduced that provide a more detailed semantic description of the situation being modeled [Smith77, Hammar78, Navathe78]. In these papers, constructs are introduced to represent subsets of entity classes in the data model. These subsets have a semantic significance in the data model, such as certain identifying properties that make them different from other entities in the class,
The requirement to have a model which describes the data relationships independently of implementation concerns was recognized when standardization of the CODASYL model was suggested. The ANSI/X3/SPARC committee [Steel75] described a DBMS architecture in response to the perceived long range needs. A principal component of the architecture is the concept of a schema, which is to contain essential information about the database itself. The conceptual schema would be augmented by an internal schema to define the implementation, and by possibly several external schemas to represent the transformations of the database to the views desired by the users.
2. PURPOSE OF THE STRUCTURAL MODEL

The numerous data models presented in the literature have given insight into the process of logical data model design, and the implemented relational, hierarchical and network database systems have provided experience on both logical and physical database design and implementation. The model presented here is intended to assist in the development of a conceptual data model independent of any implementation, but also to provide a framework for database implementation. We propose that the model satisfies the criteria [Kent77] for representing the relationships within the conceptual schema of a database system that has an architecture similar to the ANSI/X3/SPARC DBMS architecture.

The structural model which we present here:

1. avoids the storage structure dependency and the limitations of the hierarchical and network models,
2. introduces semantic information to the relational model by the representation of logical connections between relations which also define structural integrity constraints in the model itself,
3. allows a precise representation of the semantics of relationships between entity classes, and
4. provides a framework for the design of a database system starting with the design of individual users data models, to the integration of the data models to form a global database model, and finally the guidance of the choice of database implementation structures.

Associated with this structural model is a methodology to combine multiple, related data models to form an integrated database model, and to design the data models to match closely the real-world situation being represented. The individual data models also allow the user to specify some of his requirements of the database system.

The model we present is built from relations, augmented with two additional basic concepts. First we associate a relation type with each relation. Second we associate connection types with the relation types which define the structural integrity of this relation with respect to other relations that are logically related to it in the model. We define structural integrity to be the maintenance of a consistent relationship among tuples in different relations of the data model as defined by the connections among relations.

During the design and integration process, the relations will be manipulated. To assure manipulatability, we require all relations to be in Boyce-Codd normal form. However, it is not necessary to build the relations from the functional dependencies between attributes. Rather, as also argued by Chen [Chen78], if we first define the logical entities and relationships from the real-world, then simple transformations will create a model where all relations are in third normal form. Once a relation is defined with all its attributes, one can check the functional dependencies between the attributes of the relation. If a relation is not in third normal form, it may be transformed into two or more relations in third normal form [Wiederhold77, sec. 7.2]. The structural model prescribes how the data model relation and connection types will represent the entities and relationships of a particular real-world situation, and hence limits the number of possible data models that may represent a real-world situation.

We note here that the structural model is completely independent of implementation considerations. While the structural model does represent connections between relations, it does not mandate implementation of these connections. Rather, the connections are used for definition of some logical integrity constraints. An implementation can be chosen based upon an existing relational, hierarchical or network database management system, or possibly by using some other approach.
3. THE STRUCTURAL MODEL

3.1, Real-World Structures:

A database system is used to model some aspect of the real world. People approach real-world data in several phases. First, they observe the situation and collect existing data that describe the situation. Then, from their observations, they classify the data into abstractions. Next, they assess the value of their abstractions in terms of how much it helps them manage the world with a minimum of exceptions. Finally, if they have to implement a system, they describe the real-world situation by a data model. Such a model may be stored on some physical medium (computer or paper files), and used as a guide for data processing. We hence introduce a model which can be used to represent the majority of real-world situations rather than a model which may be used to represent all possible real-world semantics.

The main building blocks of the data model are classes of entities, such as PEOPLE, CARS, HOUSES, . . . etc. An entity class is described by the primitive components that are used to describe each of its members, the properties. For example, the entity class CARS can have the properties LICENSE-NUMBER, COLOR, MODEL, YEAR. The properties that identify a specific entity within the entity class, in this case the single property LICENSE-NUMBER, are called the ruling properties. The properties that describe characteristics of an entity, in this case COLOR, MODEL, and YEAR, are called the dependent properties.

Associated with each property is a domain, the set of values the it can take in any of the entities that have this property. Some properties may be repeating. For example, consider the class of entities EMPLOYEES. One of the properties we may represent is the SALARY-HISTORY of an employee. Each employee will have several entries of the salary history, one for each salary he had during his previous employment period. The number of entries is variable from one employee to the next. The SALARY-HISTORY is also an example of a compound property, one which is formed of several, more basic, other properties. In this case, SALARY-HISTORY is formed from two more basic attributes, YEAR and SALARY-VALUE. However, such compound properties can always be decomposed into several of the basic properties.

We also have to model the relationships that exist between entity classes. A relationship is a mapping among classes. Thus, a relationship defines a rule associating an entity of one class with entities of other (not necessarily different) classes. Most relationships we encounter are between two entity classes. An example of such a relationship is CAR:OWNER between the entity classes CARS and PEOPLE. Such relationships may be 1:1 (for example COUNTRY:PRESIDENT), 1:N (for example MANAGER:EMPLOYEE), or M:N (for example STUDENT: CLASS). Other relationships may be among more than two classes. For example, the relationship SUPPLIER:PART:PROJECT is among three entity classes SUPPLIERS, PARTS, and PROJECTS.

A relationship between two entity classes has two important characteristics: the cardinality and the dependency. The cardinality of a relationship places constraints on the number of entities of one class that can be related to a single entity of the other class. The dependency characteristic of a relationship places constraints on whether an entity of one class can exist that is not related to any entities of the other class. We will discuss these characteristics more fully in section 4.1.

Finally, some classes of entities may be sub-classes of other entity classes. For example, the entity class EMPLOYEES is a sub-class of the entity class PEOPLE.

The data model should reflect the real-world structure as closely as possible. This makes it easier for the users to understand the model, and allows useful semantic information from the real world to be included in the data model.
In the structural model, relations are used to represent entity classes, and some types of relationships between entity classes. Other relationships between entity classes are represented by connections between relations. Relations will be categorized into several types, according to the structure they represent in a data model. Connections between relations will also be classified into types, and possible connections between relation types are a part of the model.

Simple properties are represented by attributes of relations. We will always decompose compound properties into the simple properties from which they are formed.

3.2. Relations and Connections:

Relational concepts are well known, but for conciseness we now define relations and relation schemes as we use them in the structural model. Then we formally define the concept of connections between relations.

In order to define a relation, we first define attributes, tuples of attributes, and relation schemes. Relation schemes specify the attributes of a relation. Attributes define the domain from which data elements that form the tuples of the relation can take values.

We will use $B, C, D, b, c, d, x, y, z$ to denote single attributes; $X, Y, Z, \mathcal{B}, \mathcal{C}, \mathcal{D}$ to denote sets of attributes; $b, c, d$ to denote values of single attributes; and, $x, y, z$ to denote tuples of sets of attributes. For simplicity, we assume that all sets of attributes are ordered.

3.2.1. Relations:

**Definition 1:** An attribute $B$ is a name associated with a set of values, $\text{DOM}(B)$. Hence, a value $b$ of attribute $B$ is an element of $\text{DOM}(B)$.

For an (ordered) set of attributes $Y = \{B_1, \ldots, B_m\}$, we will write $\text{DOM}(Y)$ to denote $\text{DOM}(B_1) \times \ldots \times \text{DOM}(B_m)$, where $X$ is the cross product operation. Hence, $\text{DOM}(Y)$ is the set $\{\{b_1, \ldots, b_m\} | b_i \in \text{DOM}(B_i) \text{ for } i = 1, \ldots, m\}$.

**Definition 2:** A tuple $y$ of a set of attributes $Y = \{B_1, \ldots, B_m\}$, is an element of $\text{DOM}(Y)$.

**Definition 3:** A relation schema $R_s$, of order $m, m > 0$, is a set of attributes $Y = \{B_1, \ldots, B_m\}$. The relation, $R$, is an instance (or current value) of the relation schema $R_s$, and is a subset of $\text{DOM}(Y)$.

Each attribute in the set $Y$ is required to have a unique name.

The set $Y$ is partitioned into two subsets, $K$ and $G$. The ruling part, $K$, of relation schema $R_s$ is a set of attributes $K = \{B_1, \ldots, B_k\}, k \leq m$, such that every tuple $y$ in $R$ has a unique value for the tuple corresponding to the attribute set $K$. For simplicity, we assume the set $K$ is the first $k$ attributes of $Y$. The dependent part, $G$, of relation schema $R_s(= Y)$ is the set of attributes $G = Y - K$, where $-$ is the set difference operator.

All relations are in Boyce-Codd normal form. (For definitions of functional dependency and Boyce-Codd normal form, see section 8.1.)

We will write $R[Y]$ or $R[B_1, \ldots, B_m]$ to denote that relation $R$ is defined by the relation schema $Y = \{B_1, \ldots, B_m\}$.

Also, $K(Y)$ will denote the ruling part of relation schema $Y$, and $G(Y)$ will denote the dependent part. Similarly, for a tuple $y$ in relation $R$, defined by the relation schema $Y$, $k(y)$ will denote the tuple of values that correspond to the attributes $K(Y)$ in $y$, and $g(y)$ will denote the tuple of values that correspond to $G(Y)$ in $y$. 


A relation $R[Y]$ may have several attribute subsets $Z$ which satisfy the uniqueness requirement for ruling part. In the structural model, the ruling part of a relation schema is defined according to the type of the relation (see sec. 3.4).

3.2.2. Connections:

We now define the concept of a connection between two relations, then define the types of connections that are used in the structural model. A connection is defined between two relation schemes. An instance of the connection exists between two tuples, one from each relation.

**Definition 4**: A connection between relation schemes $X_1$ and $X_2$ is established by two sets of connecting attributes $Y_1$ and $Y_2$ such that:

a. $Y_1 \subseteq X_1$.

b. $Y_2 \subseteq X_2$.

c. $\text{DOM}(Y_1) = \text{DOM}(Y_2)$.

We then say that $X_1$ is connected to $X_2$ through $(Y_1,Y_2)$.

Two tuples, one from each relation, are connected when the values for the connecting attributes are the same in both tuples.

The definition of connection is symmetric with respect to $X_1$ and $X_2$, and thus it is an unordered pair.

Connections may be more complex. For example, if we desire a connection between two sets of attributes with dissimilar, but related, domains, condition (c) above may by changed to $\text{DOM}(Y_1) = f(\text{DOM}(Y_2))$. The function $f$ will relate values of data elements from the two domains. The equality condition in (c) above is the simplest case.

The structural model uses three basic types of connections, which we now define. Associated with each of the connection types are a set of integrity constraints that define the existence dependence of tuples in the two connected relations. These constraints define the conditions for the maintenance of the structural integrity of the model. We will define structural integrity, and discuss these constraints in section 3.5.

**Definition 5**: A reference connection from relation schema $X_1$ to relation schema $X_2$ through $(Y_1,Y_2)$ is a connection between $X_1$ and $X_2$ through $(Y_1,Y_2)$ such that:

a. $Y_2 = K(X_2)$.

b. $Y_1 \subseteq K(X_1)$ or $Y_1 \subseteq G(X_1)$, but $Y_1$ may not contain attributes from both $K(X_1)$ and $G(X_1)$.

**Definition 5a**: A reference is an identity reference if $Y_1 = K(X_1)$.

**Definition 5b**: A reference is a direct reference if it is not an identity reference.

Reference and direct reference are not defined symmetrically with respect to $X_1$ and $X_2$, and thus are ordered pairs $(X_1,X_2)$ when the reference is from $X_1$ to $X_2$. The identity reference is defined symmetrically, but we still consider it to be ordered. This is because identity references are used to represent a subrelation of a relation, defined in section 3.4.2, and we consider the reference to be directed from the subrelation to the relation.

**Definition 6**: An ownership connection from relation schema $X_1$ to relation schema $X_2$ through $(Y_1,Y_2)$ is a connection between $X_1$ and $X_2$ through $(Y_1,Y_2)$ such that:

a. $Y_1 = K(X_1)$. 

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The ownership connection is also non-symmetric with respect to $X_1$ and $X_2$, and is an ordered pair $\langle X_1, X_2 \rangle$ when the ownership connection is from $X_1$ to $X_2$.

The connections defined above may be represented graphically as in figure 1. They are represented by directed arcs, with the representing the end of the connection. The ruling part attributes in each relation arc marked $K$, and separated from the dependent part attributes by double lines ($\parallel$).
3.3. Type8 of relations:

Relations in the structural model are classified into structural types, which define their interaction with other relations in the data model. Relations can also be classified semantically according to the concept they represent from the real-world situation. One should be careful to distinguish between the semantic and the structural role of a relation in a data model.

Semantically, we distinguish between classes of entities, properties of classes of entities, and relationships among classes of entities. Classes of entities can be represented by several structural relation types, depending upon their relationship with other classes of entities. Hence, entity classes may be represented by either primary entity relations, referenced entity relations, or nest relations, as we shall see.

Non-repeating properties of a class of entities are represented as attributes of the relation that represents the entity class. Repeating properties of a class of entities are represented by a nest relation owned by the relation that represents the entity class (see section 3.3.3).

Relationships among entity classes can also be represented using different structures, depending upon the characteristics of the relationship. A relationship between two entity classes may be represented by an ownership connection, a reference connection, or two connections and an auxiliary relation. This auxiliary relation may be a primary relation, a nest relation, or an association relation (see section 4.1).

Structurally, relations are categorized into five types: primary relations, referenced relations, nest relations, association relations, and lexicon relations. These are all relations which have the same form, but are classified according to their connections to other relations.

In this section, we informally present the rationale behind the choice of the different structural relation types. We give formal definitions for the relation types in section 3.4.

A relation in the data model which represents a class of entities in the real-world situation is termed an entity relation. The choice of entity classes is a fundamental aspect of the data model design process. The goal is to match entity relations as closely as possible to real-world entity classes.

Structurally, entity relations may be primary, referenced or nest relations. The choice of structural type to represent an entity relation depends upon its role in the data model. In the following three sections, we discuss the criteria for this choice.

3.3.1. Primary entity relations:

An important objective of the data model is to represent real-world entities. The existence of a tuple in the data model which represents such an entity is hence determined by the existence of the actual entity, independently from other modelling considerations. Classes of such entities are represented in the data model by primary entity relations. Examples of primary entity relations are EMPLOYEES and CARS. Primary entity relations should be chosen to be update-independent of other relations in the data model. An update of another relation should not require an update of a primary entity relation. An update of an entity relation, however, may require updates to other relations connected to it, as we shall see later.

An example of a primary entity relation is the relation EMPLOYEES in a model that represents a company. Updates to the EMPLOYEES relation occur only from outside the database. An employee tuple is inserted whenever a new employee is hired by the company, and deleted whenever an employee leaves. This potentially affects several other relations in the database such as CHILDREN and EMPLOYEES-DEPARTMENT. Thus, insertion of an employee tuple involves the possible addition of tuples to other relations in the database that are connected to the employee relation, such as tuples that represent the employee’s children in the CHILDREN relation, and tuples associating the employee with the departments he works for in the EMPLOYEES-DEPARTMENT relation.
relation. Note that the number of additional tuples added to the database because of the insertion of a new primary entity tuple is variable, and determined externally; the model only presents the user with guidelines to follow when inserting a primary entity tuple.

The deletion of a tuple from a primary entity relation may imply the deletion of related tuples from other relations in the database. Thus, the deletion of an employee tuple will involve the deletion of tuples for his children from the CHILDREN relation, as well as tuples associating him with the department he worked in from the EMPLOYEES-DEPARTMENT relation. Such a deletion does not involve any additional checking before the tuple is deleted, since a primary entity relation may not be referenced by any other relation in the data model.

3.3.2. Referenced entity relations:

When representing a real-world situation, one often encounters abstractions that are used mainly to describe properties of other entities. Such entities are referenced by other entities in the model. This type of entity is a referenced entity, and classes of such entities are represented in the data model by referenced entity relations. Examples of referenced entity relations are CAR MODEL SPECIFICATIONS, referenced by the attribute MODEL in the relation CARS, and JOB DESCRIPTION, referenced by the JOB attribute of the relation EMPLOYEES. The use of these referenced entities greatly reduces redundancy in the data model. As we shall see, the main difference between a primary entity relation and a referenced entity relation in the structural model is in their update characteristics.

A direct reference connection will exist from some relations in the data model, termed the referencing relations, to the referenced entity relation. The reference connection restricts the deletion of tuples in the referenced entity relation, as well as the insertion of tuples in the referencing relations. We discuss these restrictions here in terms of an example, and will define them precisely in section 3.4.

An example of a referenced entity relation is presented with respect to a company database. Suppose the company wishes to keep track of current and possible suppliers for inventory items. The SUPPLIERS relation is a referenced entity relation. The existence of supplier tuples is determined by a selection from the real-world, since the company maintains a list of its current and possible suppliers. However, a supplier tuple may not be deleted while it is being referenced from the INVENTORY relation within the data model. Thus, the deletion of tuples from a referenced entity relation requires checking the tuples in all relations in the data model which reference this referenced entity relation. Addition of tuples to the referencing relation, the INVENTORY relation in this case, is restricted to those tuples that reference an already existing supplier, represented by a tuple in the SUPPLIERS relation in the database. Thus, the name of a supplier for a new inventory item should exist in the SUPPLIERS relation before the new referencing tuple is added to the INVENTORY relation.

Tuples of referenced entity relations may be referenced from more than one relation. For example, the SUPPLIERS relation, may be referenced from the ACCOUNTS-PAYABLE relation, describing unpaid bills, as well as from the INVENTORY relation. Note that supplier tuples may exist which are not currently referenced from other tuples in the database, but one cannot delete a supplier tuple without checking tuples in all relations that may reference the SUPPLIERS relation.

All other update characteristics for referenced entity relations are the same as the update characteristics for primary entity relations. In the rest of this paper, when we use the term entity relation without qualification, we will mean primary or referenced entity relation.

3.3.3. Nest relations:

Hierarchical dependencies occur frequently in real-world situations. Hence, real-world entities will be represented in the data model whose existence directly depends upon the existence of
another entity. For example, in a company database, the CHILDREN relation represents children of employees currently working in the company. The existence of children tuples in the Company database is justified while their parent works for the company, and the tuple representing the parent exists in the EMPLOYEES relation. Such entities will be represented in the data model by nest relations.

A nest relation always corresponds to a 1:N relationship between two data model relations, the owner relation and the nest relation. In our example, the EMPLOYEES relation is said to own the CHILDREN relation. This 1:N relationship is represented in the data model by an ownership connection from the owner relation to the nest relation.

For each tuple in the owner relation, a set of zero or more tuples will exist in the nest relation that are connected to this tuple. The existence of this set of tuples depends upon the existence of the owner tuple in the owner relation. The term ‘nest relation has been chosen because each owner tuple will own a ‘nest’ of tuples in the nest relation. The existence of individual tuples of the nest is determined by the real-world requirements.

Hierarchical dependencies also occur when a class of entities has a repeating property, where the number of repetitions is variable for each entity in the class. We then represent the repeating properties by attributes in a nest relation that is owned by the relation representing the entity class. An example is the education history attributes of an employee in the company database. Here, the EMPLOYEES relation owns the nest relation EDUCATION HISTORY. In the structural model, the normalization to first normal form forces the use of distinct nest relations, but the Connection to the owner relation remains recognized.

Insertion of a tuple in a nest relation is contingent upon the existence of the owner tuple in the owner relation. Thus, one may not insert a child or an education history tuple without a corresponding owner employee tuple in the EMPLOYEES relation. The deletion of a tuple from a nest relation is not restricted by the ownership connection. The deletion of a tuple from the owner relation requires deletion of the nest of tuples owned by it in the nest relation. Insertion of tuples in the owner relation may involve the creation and insertion of a nest of tuples in the nest relation.

3.3.4. Lexicon Relations:

A lexicon relation is used to represent a one-to-one correspondence between two acts of attributes. Most frequently, the one-to-one correspondence will be between only two single attributes, but sets of attributes may also be involved. Examples are the one-to-one correspondence between the two attributes DEPARTMENT-NAME and DEPARTMENT-NUMBER in a company data model, or that between the two sets of attributes \{INSTRUCTOR, CLASS, SECTION\} and \{ROOM, HOUR, DAYS\} in a university data model. This one-to-one correspondence reflects a similar correspondence between properties.

Such one-to-one correspondences between two sets of attributes occur frequently, and isolating lexicons simplifies the data model considerably by transferring attributes that serve the same function into a lexicon relation. One set of attributes can represent all instances of either set outside of the lexicon itself. Which set of attributes remains in the core of the data model is left to the judgment of the model designer.

The lexicon relation will have a reference connection to it from every relation in the data model that includes either one or both of the sets of attributes in the lexicon. The reference connection may be a direct reference or an identity reference, depending on the situation.

Lexicons serve another important function in the data model. Frequently, relations will have more than one set of ruling (or key) attributes. A set of ruling attributes is guaranteed to have a unique value for any tuple in the relation, and thus any such set of ruling attributes may be used for tuple identification. In our model, each relation has one primary set of ruling attributes,
the ruling part of the relation. Other equivalent sets of ruling attributes are transferred to lexicon relations.

The use of lexicons can greatly reduce the number of possible alternatives for the data model, leading to a significant simplification of the model design process. The two sets of attributes in a lexicon relation can be treated conceptually as a single attribute in intermediate processes which lead to the design of the data model, and can thus be considered as equivalent in the data model. Hence, lexicon relations can be seen as a means of reducing the number of attributes in the core of the data model, leading to the creation of a clearer, simpler model.

3.3.5. Association relations:

We finally consider relations used to represent the interaction between two or more relations in the data model. Such relations will be termed association relations. An association relation between two relations associates with each tuple of one relation a number of tuples from the other relation (possibly none). It does not represent any existence dependency between the tuples in the different relations, but only an association between existing tuples.

An association relation of order 1 relates tuples from i owner relations. Each of the owner relations has an ownership connection to the association relation.

An example of an association of order 2 is the relation EMPLOYEE-PROJECT which relates an employee to the projects he works in, and vice-versa. Each project tuple and each employee tuple have an existence of their own, independently from the tuples in the association relation. A tuple in the association only relates an employee with a project.

An example of an association of order 3 is the SUPPLIER-PART-PROJECT relation, which relates tuples from three owner relations.

An association relation is used to represent information relevant to a relationship between entity classes. Usually, the entity classes are represented by the i independent relations. Thus, in our example, the EMPLOYEE-PROJECT association may include information about the job the employee does for the project, the percentage of time he works on the project, . . . etc. It is also possible for association relations to have no dependent information. In this case the association relation is used only for relating tuples from the owner relations together.

The update rules for an association relation and its owner relations are now self-evident: no tuple in the association relation may be created if there are no corresponding owner tuples in the owner relations, and deletion of a tuple from any owner relation causes the deletion of all tuples affiliated with it from the association. Note that the deletion rule does not affect the existence of the tuples related to the deleted tuple in the other owner relations; it only affects those tuples in the association relation that serve to relate these tuples together. Thus, deletion of an employee would not affect the existence of any of the projects he works for.

3.4. Formal definition of relation types:

In this section, we formally define the different types of relations discussed in section 3.3 in terms of their connections with other relation types in the data model. We then define subrelations of existing relations, and how a subrelation is connected to its base relation in section 3.4.2.

For the remainder of the paper, we will use the term relation for both the relation schema and the relation, since the meaning is clear from the context.

3.4.1. Basic relation types:

Semantically, relations are classified into entity and non-entity relations.
Definition 7: An entity relation is a relation $R[X]$ which defines a correspondence between members of a class of real-world entities and the tuples in $R[X]$.

The ruling part of an entity relation defines the correspondence to the class of real-world entities, while the dependent part includes the attributes that describe basic properties of the entities.

Structurally, we define five basic types of relations:

Definition 8: A primal relation is a relation that has no direct references or ownership connections to it from any other relation in the data model.

Primary relations are required to have no references or ownership connections to them. Thus, deletion of tuples from primary relations is unconstrained by the data model.

Definition 9: A referenced relation is a relation which has direct references to it from some relations in the data model.

The ruling part attributes $K(R)$ of a referenced relation, $R$, are used for referencing $R$ from other relations. Hence, each relation $R'$ that references $R$ will have a set of referencing attributes that define the reference connection to $R$. This constrains insertion and deletion of tuples in both $R$ and $R'$.

Insertion of a tuple in $R$ should precede any reference to it from a tuple in a referencing relation. Deletion of a tuple from $R$ involves checking that it is not referenced by any tuples from any of the relations that reference $R$. Insertion of a tuple in $R'$ requires the existence of all tuples that it references.

Definition 10: A nest relation is a relation, $R_2$, which has an ownership connection to it from exactly one other relation, $R_1$, in the data model. $R_1$ is the owner of $R_2$.

A nest relation $R_2$ has an ownership connection to it from the owner relation, $R_1$. Hence, the ruling part $K(R_2)$ will consist of two parts: a set of attributes to define the connection with $R_1$, and additional attribute(a) which must uniquely identify tuples owned by the same owner tuple in $R_1$.

Insertion of tuples in $R_2$ requires the existence of the owner tuple in $R_1$. Deletion of tuples from the nest relation may occur based on conditions determined externally from the database, but may also be the result of deleting an owner tuple from $R_1$, which requires deletion of all tuples owned by it in $R_2$. 
Definition 11: An association relation, $R$, of order $i > 1$, is a relation $R$ that has $i$ ownership connections to it from $i$ other relations in the data model, $R_1, \ldots, R_i$, such that:

a. each $R_j$ has an ownership connection to $R$ through $X_j, Y_j$ for $j = 1, \ldots, i$.

b. $Y_j \cap Y_k = \emptyset$ for $j \neq k$.

c. $K(R) = Y_1 \cup \ldots \cup Y_i$.

An association relation of order $i$ has $i$ ownership connections to it, one from each of the $i$ owner relations. Hence, the domain of the ruling part attributes of an association relation is a catenation of sets of attributes, each set defining the connection to one of the owner relations. A tuple in the association is owned by one tuple from each of the owner relations. For each tuple in an owner relation, there may exist zero, one, or many owned tuples in the association. Deleting a tuple from an owner relation will thus require the deletion of all tuples owned by it in the association. Insertion of a tuple in the association will require the existence of the $i$ owner tuples.

Definition 12: A lexicon relation, $R[X]$, between two acts of attributes $Y_1$ and $Y_2$ defines a 1:1 correspondence between DOM($Y_1$) and DOM($Y_2$) such that:

a. $Y_1 = K(X)$.

b. the set of attributes $Y_2$ does not appear in any relation other than $R$.

c. $Y_1 \cap Y_2 = \emptyset$, and $Y_1 \cup Y_2 = X$.

d. $R$ is referenced by one or more relations in the data model by identity or direct references.
A lexicon will have reference connections to it from all the relations in the data model that contain the set of attributes in the lexicon. The ruling part of a lexicon is the attribute set that exists in the other relations in the model, and the dependent part is the other attribute act in the lexicon. For example, if it is necessary to identify the department in several relations of the data model, then either DEPARTMENT-NUMBER or DEPARTMENT-NAME would be chosen. To simplify the model, an arbitrary single choice is made, say to use the attribute DEPARTMENT-NUMBER in all relations of the model. Then, DEPARTMENT-NUMBER will be the ruling part of the lexicon, and DEPARTMENT-NAME will be the dependent part. Every relation containing the attribute DEPARTMENT-NUMBER will reference the lexicon.

The above definitions define the five structural types of relations: primary, referenced, nest, association, and lexicon. Connections can exist at any level in the model: nest relations can be owned by other nest relations, by associations, or by referenced entity relations as well as by primary entity relations. Similar choices exist for referenced relations, associations, and lexicons. A subrelation may be defined on any relation. In the following section, we define subrelations.

3.4.2. Subrelations:

A subrelation S of some relation R defines a subset of the tuples in R as belonging to the subrelation. This subset of tuples either has a semantic significance in the data model, or has certain additional properties that have to be represented, but that are not represented in the other tuples in R. The relation R is called the base relation of the subrelation S.

We will not allow duplication of information in the representation of a subrelation, other than the information needed for tuple identification. Hence, a subrelation will have the same ruling part attributes as the base relation, and will be connected to the base relation through an identity reference connection. The identity reference reflects the fact that a tuple in the subrelation that has the same value for the ruling part as a tuple in the base relation represents the same entity in the data model.

All attributes other than the ruling part attributes of the subrelation have to be different from the attributes of the base relation.

**Definition 13:** A (non-restriction) subrelation of relation R[X] is a relation S[Z] such that:

a. an identity reference exists from S to R.

b. for every tuple z in S, there exists a corresponding tuple x in R such that k(x) = k(z).

c. Z - K(Z) \cap X - K(X) = ∅.

The relation R is called the base relation for subrelation S.

**Definition 13a:** A restriction subrelation of a relation R[X], restricting the set of attributes Y, Y C X, to the subdomain D, D C DOM(Y), is a subrelation S[Z] of R such that: for every tuple x in R that has as value for the set of attributes Y a tuple y in D, there exists a corresponding tuple z in S such that k(z) = k(x).

An example of a restriction subrelation is a relation TECHNICAL EMPLOYEES, a subrelation of the EMPLOYEES relation, restricting the attribute JOB of EMPLOYEES to the subdomain (engineer, researcher, technician), say.

Existence of tuples in a restriction subrelation is totally dependent on the existing tuples in its base relation. In our example, all employee tuples with job value engineer, researcher or technician must also exist in the TECHNICAL EMPLOYEES subrelation, while all other employee tuples cannot exist in this subrelation.

An example of a non-restriction subrelation is a relation EMPLOYEES IN SPECIAL PROJECT X. Existence of tuples in this subrelation is determined externally of the data model, but confined to tuples in the base relation of all employees.

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We will use subrelations to represent three cases:

1. When a subset of a relation has a semantic significance within the data model, or has additional attributes that need to be represented in the model.
2. When integrity constraints require a subset of a relation to own a nested relation or an association, or to be referenced from another relation.
3. When we combine data models to form an integrated database model (see section 5), some data models may represent subsets of relations represented in other data models. This has to be reflected in the integrated database model.

The update rules for the base relation and the subrelation are: when a tuple that belongs to the subset represented by the subrelation is inserted in (deleted from) the base relation, the corresponding tuple (having the same ruling part value) is inserted in (deleted from) the subrelation. Also, if an update to a tuple in the base relation results in the removal of the tuple from the subset, the corresponding tuple should be deleted from the subrelation. For example, if the job of an employee tuple is changed from engineer to manager the corresponding tuple in the TECHNICAL EMPLOYEES subrelation should be deleted.

### 3.5. Maintaining the structural integrity of the data model:

Structural integrity exists in our model when the tuples in the data model do not violate the constraints specified by the connections between relations. One can consider that the structural model contains a basic set of integrity assertions as part of the model. The integrity assertions are those expressed implicitly by the connections between relations, and are used to specify the existence dependencies, and hence the update constraints, of tuples in connected relations.

We do not specify in the model when or how the integrity constraints are to be maintained in an implementation of the data model. The purpose of the model is that integrity constraints can be recognized, and that implementors can refer for guidance to the model. In practical implementations, there may be intervals where the structural integrity rules do not hold. It should be known however which structural integrity constraints have been violated and are awaiting correction. Hierarchical and network databases tend to require that all integrity constraints be satisfied for those connections that are actually implemented. Techniques dealing with temporary integrity violations using artificial reference tuples are indicated in [Wiederhold77].

Our model may appear less powerful than the original relational model since update integrity violations can occur. In the pure relational model, inter-relation connections are not described, but are left to be discovered at query-processing time. The lack of recognition of logical connections between relations in a database model will simplify certain technical problems during update, but does not eliminate semantic inconsistencies relative to knowledge models of the database administrator or the user. Furthermore in many situations it is best to discover and correct integrity violations at the time of update rather than to try and cope with an inconsistent database at query processing time.

In section 3.5.1, we list the integrity constraints specified by each connection type, then give a summary of rules for maintenance of the structural integrity for each of the relation types. We then show in section 3.5.2 how these rules may be expressed as simple algorithms for maintaining the structural integrity of the database upon insertion and deletion of tuples, and update of attribute values.

#### 3.5.1. Update constraints in the structural model:

The integrity constraints specified by the connection types are the following:

**A direct reference connection** from relation \( R_1 \) to relation \( R_2 \) specifies the constraints:

1. Every tuple in \( R_1 \) must reference an existing tuple in \( R_2 \).
(2) Deletion is restricted for tuples in $R_2$. Only tuples that are not referenced from any relation in the data model may be deleted.

An **ownership connection** from relation $R_1$ to relation $R_2$ specifies the constraints:

1. Every tuple in $R_2$ must be owned by an existing tuple in $R_1$.
2. Deletion of a tuple from $R_1$ requires deletion of all owned tuples in $R_2$.

An **identity reference connection** from a subrelation $R_1$ to its base relation $R$ specifies the constraints:

1. Every tuple in $R_1$ must reference an existing tuple in $R$.
2. Deletion of a tuple from $R$ requires deletion of the referencing tuple in $R_1$.
3. If $R_1$ is a restriction subrelation, then every tuple in $R$ that belongs to the subrelation (specified by the value of the restricting attributes in $R$) must exist in $R_1$.

We now give an informal listing of the update constraints associated with each relation type:

1. Primary relation:
   (a) The tuples are neither owned nor referenced by other tuples in the data model.
   (b) Deletion of a tuple requires the deletion of tuples owned by it in nest and association relations.
   (c) Insertion of a tuple requires the existence of referenced tuples in the relations referenced by attribute values in the new tuple.

2. Referenced relation:
   (a) The tuples are referenced from other tuples in the data model.
   (b) The ruling part defines the attributes through which the tuples are referenced by other tuples in the data model.
   (c) Deletion of a tuple is constrained by the existence of references to that tuple. Also, as in 1(b)
   (d) As in 1(c)

3. Nest relation:
   (a) The tuples may be referenced from other tuples in the data model.
   (b) The ruling part defines a specific owner tuple, and a specific tuple within the nest of tuples that has the same owner tuple.
   (c) As in 1(b). If the relation is referenced, deletion is constrained by existence of references to the tuple.
   (d) Insertion of a tuple requires the existence of the owner tuple in the owner relation, and the existence of referenced tuples in relations referenced by it.

4. Lexicon relation:
   (a) As in 2.a.
   (b) The ruling part is a set of attributes, through which the tuple is referenced.
   (c) Deletion of tuples is constrained by the existence of references to that tuple.
   (d) Insertion of a tuple requires no checking.

5. Association relation of order $i$:
   (a) As in 3.8.
   (b) The ruling part defines $i$ specific owner tuples, one from each of the $i$ owner relations.
(c) A6 in 3.c.
(d) Insertion of a tuple requires the existence of the i owner tuples in the i owner relation, and
the existence of referenced tuples in relations referenced by it.

8. Subrelation:
(a) A6 in 3.8.
(b) The ruling part attributes are used for referencing the base relation through an identity
reference.
(c) A6 in 3.c.
(d) Insertion and deletion of tuples in a restriction subrelation are totally controlled by existing
tuples in the base relation.

As indicated earlier, a relation may have more than one connection with other relations in
the data model. A nest relation may for instance itself be referenced, and may also reference tuples
of another referenced entity relation. In these cases, all connections impose constraint6 on the data
model.

3.5.2. Data model update algorithms:

We now give three simple algorithm6 for maintaining the structural integrity of the data
model by observing the constraints given in the preceding section. The algorithm6 will be described
in terms of the connection types defined in section 3.2.2.

3.5.2.1. Tuple insertion algorithm:

Upon receipt of a request to insert a new tuple x in relation R:

a. Check the consistency of the new tuple with the current tuples in the database:

a.1. For every relation R1 referenced by R through a reference connection, verify that
the tuple y referenced by x exists in R1.

a.2. For every relation R1 that has an ownership connection to R, verify that the owner
tuple y of x exists in R1.

b. If the new tuple is consistent with the data model, insert it and for every relation R2 owned
by R through an ownership connection, send a message to the user reminding him to insert
the tuples owned by x in R2.

Thus insertion involves two actions: checking that tuples connected with the new tuple exist
in the data model, and insertion of other tuples connected with the new tuple. The checking can
be done automatically, but insertion of other new tuples will in most cases be done by the user.
For example, the insertion of an employee tuple involves insertion of his children in a nest relation
CHILDREN owned by the EMPLOYEES relation, and of the tuples associating the employee with
the department he work6 for in the EMPLOYEE-DEPARTMENT association relation, also owned
by EMPLOYEES. However, any new tuples in both CHILDREN and EMPLOYEE-DEPARTMENT
are inserted by the user. The system only reminds the user that such data may exist, and if they
do exist they should be added to the data model.

In some cases, a6 when a nest relation represents repeating properties of an entity class, an
application program can be written to insert all properties of the entity simultaneously. Both a
tuple in the entity relation, and it6 nest of tuples that represent the repeating property are inserted.

3.5.2.2. Tuple deletion algorithm:

Upon receipt of a request to delete tuple x in relation R:


a. Check for direct references to \( x \) from other tuples in the database: If relation \( R \) is a referenced relation or a lexicon, check that \( x \) is not referenced by any tuple from a relation with a direct reference to \( R \). If \( x \) is referenced, send an error message, and do not complete the deletion.

b. Check if tuples owned by \( x \) may be deleted: For every relation \( R_1 \) owned by \( R \), initiate deletion of the tuples in \( R_1 \) owned by \( x \). For every subrelation \( R_2 \) of \( R \), initiate deletion of the tuple \( y \) in the subrelation that corresponds to \( x \).

c. If all the owned and subrelation tuples can be deleted, complete deletion of \( x \). Otherwise, do not complete deletion of \( x \), and send a warning message that \( x \) could not be deleted.

Deletion also consists of two parts: checking that the tuple being deleted is not referenced, and deleting tuples owned by the tuple being deleted. The algorithm is recursively applied.

3.5.2.3. Attribute update algorithm:

Upon receipt of a request to update attribute \( A \) of tuple \( x \), which belongs to relation \( R \):

a. If \( A \) is neither an attribute through which \( R \) references other relations, nor a member of the ruling part of \( R \), perform the update.

b. Update of connection attributes:

b.1. Referencing attributes: If \( A \) is an attribute through which \( R \) references a relation \( R_1 \), check that the new value will reference an existing tuple in \( R_1 \). If the new value references a non-existing tuple in \( R_1 \), do not complete the update and send an error message.

b.2. Ruling part attributes: If \( A \) is a member of the ruling part of \( R \), initiate deletion of \( x \) using the deletion algorithm. If deletion is completed, insert the updated tuple \( x_1 \) with the new value for \( A \) using the insert algorithm. Otherwise, send an error message.
4. REPRESENTATION OF DATA MODELS

We now present the guidelines that the structural model presents to a data model designer, and discuss how a choice is made between the different representation forms provided by the structural model to represent a particular situation. We will see that the same data can be represented with different relationships, according to the situation, or the view of the data model designer. Eventually such differences can be accommodated in the integrated database model.

We use the following notation to represent connections in our diagrams:

```
Ownership connection  Direct reference  Identity reference
```

4.1. Representation of relationships in the structural model:

One of the advantages of the structural model is that it guides the choice of representation for a particular situation. This is because the rules attached to each relation and connection type are explicit, and will lead the data model designer to carefully consider the situation he is modelling. A model relevant to the real-world situation will be the result, and the situation will be clearly represented.

In the ensuing discussion, we use the term relationship to denote a relationship between two real-world entity classes, and the term connection to denote a connection between two relations in a data model.

Consider the relationship between two entity classes, FATHERS and CHILDREN. This is a 1:N relationship, and may be represented using several different constructs in the structural model (figure 5):

a. An association between two entity relations representing fathers and children.
b. A direct reference, from an entity relation representing children, to a referenced entity relation representing fathers.
c. An ownership connection, from an entity relation representing fathers, to an entity relation representing children.

The choice among these alternatives depends upon the situation being modelled.

First, consider the case where the data model represents a community of people. Each person in the community has an identity of his own, and we want to represent the father-child relationship between two persons in the community. In this case, the appropriate representation would be an association between two persons, the FATHER-CHILD association relation (figure 5a). If either the father or his offspring move from the community, there is no further need for a father-child connection between two persons in the community. This is well represented in the data model by the association, since deletion of a father (or child) tuple causes the deletion of the associating tuple, but leaves the tuple representing the other person unaffected.

On the other hand, suppose the data model represents data from a school system. In this case, the father-child relationship is best represented by a reference connection from a CHILDREN relation to a FATHERS relation (figure 5b). This restricts the deletion of a father tuple as long as it is being referenced by a child tuple. Again, this is a faithful representation of the situation since we want to keep information on the father as long as he has a child in the school. Also, every
child in this school must have some information about his father. (If the father is unknown, an “unknown father” tuple could be placed within the FATHERS relation.)

Finally, if the data model represents data from a company, and a child is represented in the data model only because his father works for the company, then the relationship is best represented as a nest relation CHILDREN owned by the FATHERS relation (figure 5c). (In this case, FATHERS could be a superset of the EMPLOYEES relation.) Then, children are automatically deleted from the data model once their father is deleted. Here, when an employee is fired (and the decision is made to remove his representation from the active employees file), the company is not interested in any information about his children.

Let us consider a second example, that of an inventory allocation. The situation being represented is the association between suppliers, parts and projects. If each of the three entity classes has an independent existence of its own, the appropriate representation is an association among three entity relations SUPPLIERS, PARTS and PROJECTS (figure 6a).

Alternatively, suppose that we want to associate with each supplier the part(s) that he supplies, 60 that a part does not have an independent existence, but depends on the supplier that supplies the part. Then, the situation is best represented by two entity relations, SUPPLIERS and PROJECTS, a nest entity relation PARTS owned by the SUPPLIERS relation, and an association relation PARTS-PROJECTS between PARTS and PROJECTS (figure 6b). Note that this represents the full association of SUPPLIER:PART:PROJECT, since by the definition of a nest relation, the ruling part of the nest relation PARTS includes the ruling part of the SUPPLIERS relation (see section 3.4.1).

These two examples show how the update rules associated with each relation type are used for guidance when designing a data model. The update rules force the data model designer to carefully consider the characteristics of the situation that he is modelling, and thus the data model becomes a faithful representation of the situation.
4.2. Representation of a relationship between two entity classes:

In this section, we consider all possible ways in which the structural model can represent a relationship between two entity classes. This is important for identifying the constraints on relationships. It is also important when we discuss data model integration in section 5.

Consider two entity classes, A and B, related in some way. One characteristic of the relationship is its cardinality. The cardinality of the relationship restricts the number of entities of one class that may be related to an entity of the other class. The cardinality of the relationship between A and B may be:

(a) 1:1, an entity in A may be related to at most one entity in B, and vice versa.
(b) 1:N, an entity in A may be related to N entities in B, \( N \geq 0 \), but an entity in B may be related to at most one entity in A.
(c) M:N, an entity in A may be related to N entities in B, \( N \geq 0 \), and an entity in B may be related to M entities in A, \( M \geq 0 \).

Cardinalities may be further constrained by specifying \( M \) and \( N \) as constant numbers. For example, a 1:1 relationship is a constrained 1:N relationship with \( N \) set to 1.

The second characteristic of relationships is the dependency. The dependency specifies whether an entity of one class can exist independently, or whether it must be related to an existing entity of the other class. Dependencies can be classified into three types:

(a) A total dependency specifies that entities in both classes must be related to a specified number of entities of the other class at all times.
(b) A partial dependency specifies that entities from one class, entity class A say, must be related to a specified number of entities of the other class, B here, but that entities in B can exist independently.
(c) A no dependency specifies no dependency constraints.

A direct relationship between the two entity classes A and B may be represented in the structural model as one of five choices (figure 7):

(1) A reference connection: entity class A is represented as a relation \( R_a \), referencing the relation \( R_b \) that represents entity class B (figure 7a). The cardinality of the relationship A:B is \( N:1, N \geq 0 \), and the dependency is partial of A on B (each entity in A must be related to exactly one entity in B).
(2) An ownership connection: entity class A is represented by a relation \( R_a \) that owns a nest relation \( R_b \) representing entity class B (figure 7b). The cardinality of the relationship A:B is \( 1:N, N \geq 0 \), and the dependency is partial of B on A (each entity in B must be related to exactly one entity in A).
(3) An association relation: relations \( R_a \) and \( R_b \) represent entity classes A and B, and an association relation \( R_{ab} \) represents the relationship (figure 7c). The cardinality of the relationship A:B is \( M:N, M \geq 0, N \geq 0 \), and there is no dependency.
(4) A nest of references: relations \( R_a \) and \( R_b \) represent the entity classes A and B. A nest relation \( R_{ab} \) owned by \( R_b \) and a reference connection from \( R_{ab} \) to \( R_b \) represent the relationship (figure 7d). The cardinality of A:B is \( M:N, M \geq 0, N \geq 0 \), and there is no dependency.
(5) A primary relation and two reference connections: relations \( R_a \) and \( R_b \) represent the entity classes, and the relationship is represented by a primary relation \( R_{ab} \) and two reference connections from \( R_{ab} \) to \( R_a \) and \( R_b \) (figure 7e). The cardinality of A:B is \( M:N, M \geq 0, N \geq 0 \), and there is no dependency.

Other relationships may exist indirectly. For example, if entity classes A and B, and entity classes B and C are directly related, an indirect relationship exists between entity classes A and C. We will only further consider direct relationships in this report.
Data models that represent the same two related entity classes may use different representations for the relationship according to the way they view the update constraints. Two reasons for choosing different representations can be distinguished: difference in understanding and difference in representation. We illustrate the differences with an example.

(1) The two data models differ in their understanding of the same real-world situation. Consider the two entity classes DEPARTMENTS and EMPLOYEES. It is possible that one user assumes that the relationship between DEPARTMENTS and EMPLOYEES is 1:N (each employee works in only one department). A second user is aware of exceptions and considers the relationship M:N (an employee may work in more than one department). A disagreement exists about the actual situation being modeled, and one of the data models is in error. It may be that the first user knows only about employees that work in one department. If such a conflict occurs between the two data models, the real-world situation being modeled must be re-examined to determine its actual characteristics. We will not consider this problem further.

(2) The two data models represent the real-world situation differently, each user choosing the representation which best suits his integrity control requirements. Consider the DEPARTMENTS and EMPLOYEES example, and suppose the relationship is of cardinality 1:N. It may be represented in one of the following ways, among others:

(a) a reference connection from EMPLOYEES to DEPARTMENTS (figure 8a),
(b) an ownership connection from DEPARTMENTS to EMPLOYEES (figure 8b,8c),
(c) an association relation restricted to 1:N (figure 8d),
(d) a nest of references from EMPLOYEES to DEPARTMENTS (figure 8e).

The different representations reflect different integrity requirements:

- The reference representation requires each employee represented in the data model to belong to a department, and restricts deletion of a department from the data model while it is referenced by some employee.

- The ownership connection representation also requires that each employee belongs to a department, but that deletion of a department tuple from the data model results in the deletion of all the employee tuples who work in that department.

- The association does not place any constraints on the existence of the actual entities represented, the employee and department tuples. However, an association can exist only between tuples represented in the data model.

Finally, the nest of references restricts the deletion of a department while referenced by some employee, but allows employee tuples to exist in the data model that are not related to any department.
Since the association representation can be used to represent \textbf{M:N} relationships, but here the DEP:EMP relationship is \textbf{1:N}, the EMP-NO attribute must have a unique value for each tuple in the association relation. This is indicated in figure 8d by marking the attribute with a (U). Note that this does not violate Boyce-Codd normal form.

The nest of references may also represent an \textbf{M:N} relationship, and to restrict it to \textbf{1:N}, we also mark the EMP-NO attribute in the connecting nest relation by a (U) (figure 8e). We will use this convention throughout the examples in section 5.

In the ownership connection representation, we must consider two cases. The identifying attribute for each EMP tuple in figure 8b is EMP-NO, and has unique values for each employee independent of his department. Hence, we mark it (U). In figure 8c, the identifying attributes for an EMP tuple are the two attributes DEP-NO and EMP-ID, where EMP-ID serves to define the employee within his department, and hence is unique within a department but is not unique over all employees.
The different views may all be equally valid, and hence more than one set of views, and corresponding semantics, has to be retained in the integrated database model so that it can serve in a variety of situations.

We now consider the problem of integrating different data models, defined by independent user groups and applications, into an integrated database model, to be used as the conceptual schema. We assume a database system architecture similar to that described by the ANSI/X3/SPARC report.
5. INTEGRATION OF DATA MODELS

We now discuss integration of data models. First we briefly define our terminology for logical database design.

A **DATA MODEL** is a representation of the requirements of a particular potential database user group or application. The definition of data models for individual user groups that expect to use the database is the first step in the design of an integrated database.

The **DATABASE MODEL** is the integrated model created by merging the individual data models. During merging, differences in view are bound to appear. The differences may be resolved by transformations of the original data models. It is possible that unresolvable conflicts will emerge among the original data models. Then management decisions have to be made to force data model changes, or to abandon the integration with respect to some data models.

A **DATABASE SUBMODEL** is the user or application view that is consistent with the integrated database model. Hence, if no conflicts occurred between a user data model and the integrated database model, the database submodel for that user will be the same as the data model. If some conflict had arisen, some differences will exist between the data model and the database submodel.

In section 5.1 we consider some general concepts of data model integration, and in section 5.2 we consider the integration of relations from different data models that represent the same real-world entity class. In section 5.3 we show how to integrate two different representations of a relationship between the same two real-world entity classes.

5.1. Concepts of integration:

The data models we integrate will represent real-world situations that partially overlap, otherwise there will be no need for integration. Hence we expect to discover relations in separate data models that represent the same entity classes. The first phase of integration is to recognize such relations. This is not always a simple task, since different data models may use different names for relations that represent the same entity class.

Recognition of relations that represent the same entity class in different data models is based on matching ruling parts, since the ruling part defines the correspondence to an entity class. The relation names and the ruling part attribute names can provide an initial hint to such correspondences. If data exists, similar values within the ruling part attributes can further indicate candidates for entity matching. A match or overlap of the domain definition of ruling part attribute can establish the necessary equivalence.

Ruling parts may be translated via lexicons, so the search for similar ruling parts must also consider lexicons of ruling part in the data models. Since lexicons preserve the identity of ruling parts, we will not specify throughout that lexicons can be used in the matching of ruling parts. Some examples of equivalence through lexicons will be given in section 5.2.

We assume in this report that rigorous definitions exist for the domains that the attributes cover. Definition of domains and attribute encoding can be a major effort, but is outside the scope of this report. This problem is also addressed by people working on the requirements analysis phase of database design.

The second phase of integration, following the recognition of relations that represent the same entity classes, is the recognition of differences in the representations. These differences are of three types:

(1) Representation of different properties of the same entity class. This is reflected in different dependent part attributes in the relations that represent the same entity class.
(2) Representation of different subsets of entities of the same entity class. This is reflected in different tuples in the relations that represent the same entity class.

(3) A combination of (1) and (2).

We will cover integration of those cases in section 5.2.

The final phase is to integrate the representation of relationships between two entity classes. As shown in section 4.2, there are five ways to represent direct relationships in the structural model. Data models may choose to represent the relationship between the same two entity classes differently, according to their view of the situation. Hence, the final phase of integration is to create an integrated database model which will support different representations of relationships in the data models. We cover this phase in section 5.3.

Many data models may have to be integrated into a single database model. To avoid excessive complexity we will analyze the integration of only two data models in detail. Successive integration steps can merge another data model with the database model being built, creating a new database model. Since both data models and database models use the same primitives, this should not pose a problem.

We hence have two data models, data model 1 (dml) and data model 2 (dm2). Both data models will include relations that represent some common entity classes, as well as other classes of data. We only look at one entity class A in section 5.2, and two entity classes A and B with a relationship between them in section 5.3. We will denote the relations that represent entity classes A and B in dml and dm2 by $R_A$ and $R_B$. If both representations are the same, clearly there is no need for any transformation, and the integrated database model (idbm) will use the same representation. If representations differ, we create an idbm to support both data models.

The idbm will then support database submodel 1 (dbsm1) and database submodel 2 (dbsm2), corresponding to dml and dm2 respectively. In most cases, dml and dm2 will not be changed, so dbsm1 and dbsm2 will be equivalent to dml and dm2. In some cases, where conflicts appear, one of the data models may have to be changed, and the corresponding database submodel will reflect those changes. When the database model is established, it may also be desirable for pragmatic reasons to change a database submodel to achieve a better agreement with the database.

In some cases, only a subset of the tuples in relation $R_A$ (or $R_B$) in the idbm correspond to the $R_A$ (or $R_B$) relation included in dml or dm2. We then use a subrelation to represent the subset, and an identity connection will join it to $R_A$ in the idbm. For example, if $R_A$ in dml corresponds to a subrelation of $R_a$ in the idbm, we denote this subrelation by $R_{a1}$ in the idbm, and $R_{a1}$ will have an identity reference to $R_A$. This subrelation $R_{a1}$ of $R_a$ contains only the ruling part attributes of $R_a$, so that no duplication of information occurs in the idbm. All other attributes in $R_a$ can be accessed through the identity reference to $R_a$.

We do not address the problem of authorization of users to perform insertion and deletion. We assume that every database submodel has complete insert, delete, and update authorization over the part of the database model it represents. Hence, if one submodel, dml say, inserts a tuple that does not violate the integrity constraints of dm2, the tuple is inserted in both of them. If the tuple violates the integrity constraints of dm2, it is inserted but remains invisible to dm2. For deletion, if deletion of a tuple is legal in dml, say, but the tuple may not be deleted in dm2 because of integrity constraints, the tuple will be kept in the idbm and in dm2, but will become invisible to dm2.

After integration, dbsm1 and dbsm2 are both supported by the idbm. A mapping will exist from each submodel to the idbm. This mapping includes additional integrity rules, derived from the integration process, which will apply to the idbm. These rules are enforced when a database submodel performs an insertion, deletion, or update. We will list these additional rules with each case of integration.
5.2. Integration of different representations of entity classes:

5.2.1. Recognition of relations that represent the same entity class:

This phase of integration requires the recognition of relations included in different data models that represent the same entity class. Knowledge of the real-world situations being modeled is helpful to match relations that represent the same entity class but have different names for relations and ruling part attributes. The domain definitions of ruling part attributes will then verify the equivalence of such relations by their partial overlap or total match.

Some models may include lexicons of ruling parts for some of the relations in the model. Examination of such lexicons is necessary when matching ruling parts. For example, dml may include a relation EMPLOYEES that contains the attributes (EMP-JNAME, ADDRESS, HOME-PHONE, OFFICE, OFFICE-PHONE, DEPT), representing a directory of the employees. Data model 2, representing job information, includes a relation EMP that contains the attributes (EMP-NUMBER, AGE, JOB, SALARY, DEPT), and a lexicon relation (EMP-NUMBER, EMP-JNAME) (figure 9a). To recognize that both relations represent the same entity class of EMPLOYEES, the integrators must consider both the EMP-NUMBER and EMP-JNAME attributes from the lexicon relation in dm2 when matching the ruling part of the EMP relation to the ruling part of the EMPLOYEES relation.

5.2.2. Integration of relations that contain different attributes:

We first consider the case where one representation dominates the other. Here, dml includes a relation R1, and dm2 includes a relation R2 that represents the same entity class as R1, and contains all the attributes represented in R1, plus some additional dependent part attributes. The idbm will include a relation R that contains the set of attributes represented in R1, and a subrelation R' of R that contains the dependent part attributes represented in R2 but not in R1. The tuples in R correspond to the R1 tuples in dbsm1, while the subset of tuples in R' will correspond to the R2 tuples in dbsm2. When dbsm1 inserts a tuple, it is only inserted in R, since it does not contain the dependent part attributes of R'. The tuple is only visible to dbsm1. When dbsm2 inserts a tuple, it is inserted in both R and R', since it contains the dependent part attributes of both R and R'. Hence, the tuple is visible to dbsm2 also.

The general case is that neither relation R1 of dml nor relation R2 of dm2 contains the complete set of attributes, but each contains a set of attributes common to both models, and a set of dependent attributes unique to its model. In this case, we must create two subrelations. An example is shown in figure 9. Relation R represents the common attributes, and two subrelations R1 and R2 are used to represent the tuples in dbsm1 and dbsm2 respectively. When dbsm1 inserts an employee tuple, it is inserted in R and R1, but is invisible to dbsm2. When dbsm2 inserts the tuple with the same ruling part value, the tuple is also inserted in R2, and becomes visible to dbsm2. A check has to be performed to ensure that common attributes have the same values. Thus, the base relation R insures the integrity of data values that are common to both data models.

The lexicon relation only references R2, since it is only represented in dbsm2.

If the two data models use different ruling part attributes, and neither represents the ruling part attributes in the other data model (for example, if in figure 9a dm2 did not include the lexicon), then two solutions exist. The first solution is to change one of the data models to include the ruling part attributes of the other data model. The second solution, which involves the database administrator, is to create a lexicon in the idbm in which every new tuple is included before its insertion by either data model.

We are only dealing with the data model here. When actual databases are to be integrated, inconsistencies may exist in the data. For example, the same employee may have his department
relation $R_1$ (EMPLOYEES)

| EMP-NAME | ADDRESS | HOME-PHONE | OFFICE | OFFICE-PHONE | DEP-NO |

DM1 (directory of employees)

relation $R_2$ (EMP)

| EMP-NO | AGE | JOB | SAL | DEP-NO |

| EMP-NO | EMP-NAME |

DM2 (job information)

(a) Lexicon of a ruling part that must be considered

relation $R$ subrelation $R_2$ (subset in DBSM2)

| EMP-NAME | DEP-NO |

| EMP-NAME | AGE | JOB | SAL |

| EMP-NO | EMP-NAME |

(b) Integrated database model

Figure 9, Integration of different sets of attributes (with lexicon)

listed as ‘foundry’ in one data model, and as ‘management’ in another. This problem is a post design issue, although WC note that the structural model would not allow this inconsistency if the different submodels insert their tuples representing the same employee at different times.

WC also note that although many subrelations may exist for the same base relation in the integrated database model, this is only at the model level. At the implementation level, the base relation and all its subrelations may be placed in the same file, with a conditional field for each subrelation in each record to indicate whether the record is in the subrelation or not. It may also be worthwhile to change database submodels by making them aware of a few additional attributes to simplify the database model.

5.2.3. Integration of relations that represent different sets of tuples:

WC know consider the case where there are differences in the selection of entities to be represented. For example, if one data model, dm1, includes a relation $R_1$, and dm2 includes a relation $R_2$ that represents a subset of the tuples in $R_1$. The idbm will then include a relation $R$ and a subrelation $R_2$ of $R$ to represent the tuples in $R_2$ of dbsm2. The subrelation $R_2$ may be a restriction subrelation if the subset of tuples in $R_2$ is determined by attribute values in $R$, or a non-restriction subrelation if the subset of tuples in $R_2$ is determined externally, independent of the model.

For example, dm1 (for the payroll department) may represent all employees of a company in an EMPLOYEES relation, while dm2 (for the sales department of the company) includes the relation SALES FORCE, the employees that work in the sales department. The idbm then includes a relation EMPLOYEES, and a subrelation SALES FORCE of EMPLOYEES. If the EMPLOYEES relation contains a DEPARTMENT attribute, the subrelation SALES FORCE is a restriction subrelation on the DEPARTMENT attribute, restricting the attribute to the value sales. If EMPLOYEES does not contain a DEPARTMENT attribute, SALES FORCE would be a non-restriction subrelation. In either case, after integration, dbsm2 is only allowed access to tuples in the SALES FORCE subrelation, but could still access their attribute values from the base relation EMPLOYEES, while dbsm1 would be allowed access to all employee tuples.
The general case is that the tuple in the two relations partially overlap each other. Then dml includes relation \( R_1 \) and dm2 includes relation \( R_2 \) that represent the same entity class, such that the tuples in the two relations obey the constraints \( R_1 \cap R_2 \neq \emptyset, R_1 - R_2 \neq \emptyset \), and \( R_2 - R_1 \neq \emptyset \).

The idbm then includes a relation \( R = R_1 \cup R_2 \), and two subrelations of \( R, R_1 \) and \( R_2 \). Again, \( R_1 \) or \( R_2 \) could be either restriction or non-restriction subrelations. For example, referring to a university database, dml (representing the computer science department of the university) includes a relation CSD PROFESSORS, and dm2 (representing information about permanent faculty) includes a relation TENURED PROFESSORS. The idbm then includes a relation PROFESSORS, and two subrelations of PROFESSORS, CSD PROFESSORS and TENURED PROFESSORS. Each database submodel is allowed access to his subset, and the base relation assures the integrity of common data represented in both models.

In the last example, it is possible that the relation in each data model contains attributes common to both relations, and a set of its own attributes. Then, the base relation in the idbm will contain the common attributes, and each subrelation will contain its own additional set of attributes.

5.3. Integration of different representations of relationships:

In the following sections (5.3.1-5.3.4), we assume that we have two data models, dml and dm2, and that both data models represent two entity classes A and B, and a relationship between them. \( R_a \) and \( R_b \) will denote the relations that represent entity classes A and B. If the representation of the relationship between A and B involves an auxiliary relation (association, primary or nest relation) we will designate it \( R_{ab} \).

There are five ways of representing a relationship between two entity classes in the structural model (section 4.2). Three of these representations are not symmetric with respect to A and B (reference, nest, nest of references), and two are symmetric (association, primary). If we consider all possible combinations without looking at symmetries, the set of possible cases for combining different representations pairwise is \( 2 \times (5 + 4 + 3 + 2 + 1) = 30 \). We remove 5 cases where the representation is identical in both data models, and (5 + 4) cases because the association and primary cases are symmetric with respect to \( R_a \) and \( R_b \). Then 18 cases remain to be considered. We consider all possible combinations with the association representation first (4 cases) in section 5.3.1. We then consider the cases that remain with nest of references (8 cases, section 5.3.2), with references (4 cases, section 5.3.3), and with nest (2 cases, section 5.3.4).

5.3.1. Integration with an association:

In this section, we consider integration of an association with other representations of a relationship. In those cases, dml represents the relationship A:B as an association relation, and dm2 will use a different representation. The association may represent a relationship of cardinality \( M:N \). Our assumption (section 4.2) that both original data models accurately represent the same situation implies that the cardinality of both representations is the same. Hence, the cardinality of the relationship is restricted to the representation in dm2.

In order to demonstrate how two different data models may be integrated, we will present the integration of an association with the nest of references (figure 10a).

In this case, the only difference is that dml can freely delete tuples from \( R_a \), while in dm2 deletion is restricted by referencing tuples from \( R_{ab} \). Hence, we create two subrelations, \( R_{bp} \) and \( R_{ab} \). Those subrelations represent the tuples in \( R_b \) (and \( R_{ab} \)) of dbsml. Tuples in \( R_b \) and \( R_{ab} \) in the idbm may include some tuples deleted from dbsml, but not deleted from \( R_b \) and \( R_{ab} \) in the idbm due to the deletion constraint of the referencing in dsm2. These tuples are not visible to dbsml.
Figure 10a. Integration of association and nest of references

The database submodels now obey the following rules. Insertion and deletion in $R_a$ from either $dml$ or $dm2$ is unrestricted, as is deletion of $R_{ab}$ tuples, and unreferenced $R_b$ tuples. If $dbsml$ deletes a referenced $R_b$ tuple ($dbsm2$ may not perform such a deletion), it is only deleted from $R_{bi}$ (and the owned tuples are deleted from $R_{abi}$). These rules accurately reflect the constraints imposed by the views represented in the original data models.

For brevity, we will use the following format for each integration case. We first list the differences between the two data models, then list the additional integrity constraints that have to exist in the mapping from the database submodels to the integrated database model. When listing these additional constraints, ("relation name") will mean: do the insertion or deletion specified on "relation" if allowed by the integrity constraints of the idbm.

We will now present the demonstration case again in brief notation.

(a) ASSOCIATION AND NEST OF REFERENCES (figure 10a):

Differences:

Dml may freely delete tuples from $R_b$, while in dm2, deletion of $R_b$ tuples is restricted.

Additional constraints:

dbmsl:
insert: (1) $R_b - R_{ab}, R_{b1}$, (2) $R_{ab} - (R_{ab}, R_{abi})$
delete: (1) $R_b - (R_b), R_{b1}$

dbsml:
insert: (1) $R_b - R_{ab}, R_{b1}$, (2) $R_{ab} - (R_{ab}, R_{abi})$

The relation name to the left of the "-" refers to the database submodel, while those to the right refer to the database model. We only consider cases which need additional control from the constraints. Insert in $R_a$ of $dbsml$ hence means insert in $R_a$ of the idbm, since it is not listed. In $dbsml$, insert in $R_b$ requires insertion of the tuple in both $R_b$ and $R_{b1}$ of the idbm. Insert in $R_{ab}$ requires insertion in $(R_{ab}, R_{abi})$ in the idbm, the ( ) brackets meaning if the integrity check of the idbm will allow it, here if both owner tuples exist. In $dbsm2$, insert in $R_{ab}$ requires insertion in $(R_{ab}, R_{abi})$, which means: insert the tuple in $R_{ab}$ if the integrity check of the idbm holds (here both the owner tuple in $R_a$ and the referenced tuple in $R_b$ exist), than insert the same tuple in $R_{abi}$ (if the other owner tuple exists in $R_{b1}$).

Following each integration case, we will give an example with attributes to illustrate the integration process. Example 1 illustrates the integration of association and nest of references.
Example 1

**Figure 10b. Integration of association and reference**

(b) **ASSOCIATION AND REFERENCE** (figure 10b):

The cardinality of the relationship $A:B$ is restricted to $N:1$, since the reference cannot represent an $M:N$ relationship.

Differences:

1. In dm2, every $R_a$ tuple must reference an $R_b$ tuple, while in dml not all $R_a$ tuples have to be associated with $R_b$ tuples.

2. In dm2, deletion of $R_b$ tuples is restricted by references.

Additional constraints:

**dbsml:**

- **insert:** (1) $R_b ightarrow R_b, R_b_1$, (2) $R_{ab} ightarrow (R_{a2}, R_{ab})$
- **delete:** (1) $R_b ightarrow (R_b), R_b_1$, (2) $R_{ab} ightarrow R_{a2}, R_{ab}$

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The requirement that every \( R_a \) tuple must reference an \( R_b \) tuple in \( \text{dm2} \) leads to the creation of the subrelation \( R_{a2} \), while the unrestricted deletion of \( R_b \) tuples in \( \text{dm1} \) leads to the creation of \( R_{b1} \) (example 2).

(c) ASSOCIATION AND NEST (figure 10c):

The cardinality of the relationship \( A:B \) is restricted to \( 1:N \), since the ownership connection can only represent \( 1:N \) relationships.

Differences:

1. In \( \text{dm2} \), existence of a tuple in \( R_b \) requires the existence of the owner tuple in \( R_a \), while in \( \text{dm1} \), \( R_b \) tuples can exist independently.
2. In \( \text{dm2} \), deletion of a tuple from \( R_a \) requires the deletion of the owned tuple in \( R_b \), while \( \text{dm1} \) does not require these deletions.

Additional constraints:

\begin{itemize}
  \item \( \text{dbsm2}: \) insert: \( R_b \rightarrow (R_b, R_{b1}) \)
  \item \( \text{dbsm1}: \) insert: \( R_a \rightarrow (R_a, R_{a2}, R_{ab}) \)
\end{itemize}
Example 3

The $R_b$ tuples of $\text{dbsm2}$ are only those in $R_{b2}$ in the idbm, since they require the existence of the owner tuple. In the idbm, $R_{ab}$ will also represent the subset of $R_b$ tuples in $R_{b2}$.

Here, we must consider two examples, since the nest relation may represent different tuple identification attributes than the association. First, we consider the case where the identification is the same. In example 3, EMP-NO identifies the employee in both dbsml and dbsm2. Since the cardinality of DEPARTMENT:EMPLOYEE is $1:N$, the EMP-NO attribute must have unique values in tuples of the relations marked (U). Note that this does not violate Boyce-Codd normal form. In this case, the integration is straightforward.

In example 4, the identifying information is different. Dbsm2 uses the two attributes (EMP-NO, CHILD-NAME) as ruling part, while dbsml uses only CHILD-ID. CHILD-ID uniquely identifies every child tuple, but CHILD-NAME does not. Here, if dbsm2 does not represent the attribute CHILD-ID, he has to be made aware of it to maintain the correct mapping between CHILD-ID and CHILD-NAME on insertion of child tuples.

(d) ASSOCIATION AND PRIMARY (figure 10d):

The cardinality of the relationship $A:B$ is $M:N$.

Differences:

In dm2, deletion of $R_a$ and $R_b$ is restricted by references
Example 4

Additional constraints:

**dbsml:**
- Insert: (1) $R_a = R_a, R_{a1}$, (2) $R_b = R_b, R_{b1}$, (3) $R_{ab} = R_{ab}, R_{ab1}$
- Delete: (1) $R_a = (R_a), R_{a1}$, (2) $R_b = (R_b), R_{b1}$

**dbsm2:**
- Insert: (1) $R_a = R_a, R_{a1}$, (2) $R_b = R_b, R_{b1}$, (3) $R_{ab} = R_{ab}, R_{ab1}$

### 5.3.2. Integration with a Nest of References:

Now we consider the cases that remain with a nest of references. Dml represents the relationship $A:B$ as a nest of references, and dm2 represents it differently. The cardinality of the nest of reference representation is $M:N$, but may again be restricted by the representation in dm2. The nest of reference representation is not symmetric with respect to entity classes A and B, and so we must consider it twice with each non-symmetric representation.

(a) NEST OF REFERENCES AND NEST OF REFERENCES (figure IIa):

**Differences:**
1. Deletion of $R_b$ ($R_{.}$) is restricted in dml (dm2).
2. Deletion of $R_a$ ($R_{.b}$) in dml (dm2) requires deletion of owned tuple in $R_{ab}$ ($R_{ba}$).

**Additional constraints:**

**dbsml:**
- Insert: (1) $R_a = R_a, R_{a1}, (2) R_b = R_b, R_{b2}, (3) R_{ab} = R_{ab}, R_{ab1}, (R_{ab2})$
- Delete: (1) $R_a = (R_a), R_{a1}, (R_{ab}), (2) R_b = (R_b), R_{b1}$

**dbsm2:**
- Insert: (1) $R_a = R_a, R_{a1}, (2) R_b = R_b, R_{b2}, (3) R_{ba} = (R_{ab}, R_{ba2}, R_{ba1})$
- Delete: (1) $R_a = (R_a, R_{ab}), (2) R_b = (R_b), R_{b2}, (R_{ab})$.
Figure 11a. Integration of nested references and nest of references

Example 5

When $dbsm1$ tries to delete an $R_a$ tuple in the idbm that is referenced from $R_{ba2}$, it is only deleted from $R_{a1}$. If the tuple is not referenced from $R_{ba2}$, the tuples in $R_{ab}$ that correspond to those deleted from $R_{ab1}$ (due to the deletion of $R_a$) should also be deleted, since they no longer exist in either $R_{ab1}$ or $R_{ab2}$. $R_{ab}$ exists to ensure that the tuples associating tuples from $R_a$ with tuple from $R_b$ are consistent.

Example 5 illustrates this case.

(b) NEST OF REFERENCES AND REFERENCE (figure 11b, 11c):

Both nest of references and reference are non-symmetric, so we must examine two cases.

Case 1 (figure 11b):

The cardinality of the relationship $A:B$ is restricted to $N:1$, since the reference cannot represent an $N:M$ relationship.
Figure 11b. Integration of nest of references and reference (Case 1)

```
EMP-NO | AGE | SAL

EMP-NO | DEP-NO | DEP-NO | LOC
```

DBSM1 (nest of references)

DBSM2 (reference)

Example 6

Figure 11c. Integration of nest of references and reference (Case 2)

Differences:

A tuple in \( R_a \) in dm2 must be associated with an \( R_b \) tuple.

Additional constraints:

dbsm2:

\textbf{insert: } \( R_a - (R_a, R_{a2}) \)

**Case 2** (figure 11c):

Again, \textbf{the} cardinality of \textbf{the} relationship \( A:B \) is restricted to \( 1:N \).
Example 7

<table>
<thead>
<tr>
<th>dml</th>
<th>dm2</th>
<th>idbm</th>
</tr>
</thead>
<tbody>
<tr>
<td>![Diagram of dml]</td>
<td>![Diagram of dm2]</td>
<td>![Diagram of idbm]</td>
</tr>
</tbody>
</table>

Figure 11d. Integration of nest of references and nest (Case 1)

Differences:
1. Deletion of \( R_b \) (\( R_a \)) tuples is restricted in dml (dm2).
2. Every \( R_b \) tuple in dm2 must be related to an \( R_a \) tuple.

Additional constraints:

for \( \text{dbsm1:} \)
- insert: (1) \( R_a = R_{a1}, R_{a2} \), (2) \( R_{ab} = (R_{ab1}, R_{ab2}) \).
- delete: (1) \( R_{a} - (R_{a1}, R_{ab}), (2) R_b - (R_{b1}, R_{ab}), (3) R_{ab} - (R_{ab1}, R_{ab2}) \).

for \( \text{dbsm2:} \)
- insert: (1) \( R_a = R_{a1}, R_{a2} \), (2) \( R_b = (R_{b1}, R_{b2}, R_{ab}) \).
- delete: (1) \( R_a - (R_{a1}, R_{ab}), (2) R_b - (R_{b1}, R_{ab}), R_{b2} \).

Example 7 illustrates this case.

(c) NEST OF REFERENCES AND NEST(figures 11d, 11e):

Again, both nest of references and nest are non-symmetric, so we must examine two cases. Case 1 (figure 11d):

The cardinality of the relationship \( A:B \) is restricted to \( 1:N \), since the reference cannot represent an \( N:M \) relationship.
Differences:
(1) $R_b$ tuples may exist independently in $\text{dml}$.  
(2) Deletion of $R_b$ tuples is restricted in $\text{dml}$.

Additional constraints:
$\text{dbsml}$:
insert: $R_{ab} \cdot (R_{ab}, R_{b2})$.

$\text{dbsm2}$:
insert: $R_b \cdot (R_b, R_{ab}, R_{b2})$.
delete: $R_b \cdot (R_b, R_{b2})$.

We again consider two examples, because of the different ways the nest relation may represent the tuple identifying information. In example 8, we consider the case where the identifying information is the same.

In example 9, we now consider the case where the identifying information is different. Here, we must slightly change $\text{dm2}$ by introducing an additional attribute.  

Case 2 (figure 1lc):

The cardinality of the relationship $A:B$ is restricted to $N:1$.

Differences:
(1) In $\text{dml}$, $R_a$ tuples can exist independently, while in $\text{dm2}$ an owner tuple $R_b$ tuple must exist.
(2) In $\text{dml}$, deletion of $R_b$ tuples is restricted by references, while in $\text{dml}$, deletion of an $R_b$ tuple requires deletion of related $R_a$ tuples.
Additional constraints:

**dbsm1:**
- insert: (1) $R_b \bullet R_b, R_{b2}$, (2) $R_{ab} \bullet (R_{ab}, (R_{a2}))$.

**dbsm2:**
- insert: (1) $R_a \bullet (R_a, R_{a2}, R_{ab})$, (2) $R_b \bullet R_b, R_{b2}$.
- delete $R_b \bullet (R_b, R_{b2})$.

We will only consider **one example** for this **case**, example 10, with different identification.

(d) **NEST OF REFERENCES AND PRIMARY** (figure 11f):

The **cardinality of the relationship A:B** is $M:N$.

Differences:

In dm2, deletion of $R_a$ is restricted by references.
Example 10

Additional constraints:
dbsm1:
insert: (1) $R_a - R_a, R_{a1}$, (2) $R_{ab} - R_{ab}, R_{abl}$
delete: (1) $R_a - (R_a), R_{a1}$
dbsm2:
insert: (1) $R_a - R_a, R_{a1}$, (2) $R_{ab} - R_{ab}, R_{abl}$

5.3.3. Integration with a reference:

Dml represents the relationship $A:B$ as a reference connection from $R_a$ to $R_b$, and dm2 represents it using a different structure. The cardinality of the relationship $A:B$ is $N:1$, possibly restricted by the dm2 representation.

(a) REFERENCE AND REFERENCE (Figure 12a):

The cardinality of $A:B$ is restricted to $1:1$, since in dml it is $N:1$, and in dm2 it is $1:N$. It would be unusual to encounter these two representations of the same $1:1$ relationship. However, it can be integrated.
Figure 12a. Integration of reference and reference

Example 11

Figure 12b. Integration reference and nest (Case 1)

Differences:
(1) In dm1 (dm2), every Ra(Rb) tuple must reference an Rb (Ra) tuple.
(2) Deletion of Rb (Ra) tuples is restricted in dm1 (dm2).

Additional constraints:

dbsm1:
insert: Ra = (Ra, Rb, Ra1, Ra2).
delete: Ra = (Ra), Ra1, Ra2.

dbsm2:
insert: Rb = (Rb, Rb2, Rb1, Rb2).
delete: Rb = (Rb), Rb2, Rb1.

(b) REFERENCE AND NEST (figure 12b, 12c):

Case 1 (figure 12b):

The cardinality of the relationship A:B is N:1.
Example 12 illustrates this case by a 1:N relationship between DEPARTMENTS:EMPLOYEES.

**Case 2 (figure 12c):**

The cardinality of the relationship A:B is restricted to 1:1, since in dml it is N:1, and in dm2 it is 1:N.

Differences:
1. Every R_a tuple in dml must reference an R_b tuple, while in dm2 every R_b tuple must be owned by an R_a tuple.
2. Deletion of R_b tuples is restricted in dml.
3. Deletion of an R_a tuple in dm2 requires deletion of owned R_b tuples.
Example 13

Additional constraints:

**dbsm1:**
- **insert:** \( R_a \rightarrow (R_a, R_{a1}, R_{b2}) \)

**dbsm2:**
- **insert:** \( R_b \rightarrow (R_{b1}, R_{a}, R_{b}) \)
- **delete:** \( R_b \rightarrow (R_{b1}) \)

Example 13 illustrates this case,

(c) **REFERENCE AND PRIMARY** (fig 12d):

The cardinality of the relationship A:B is N:1.

Differences:

In dm2, deletion of \( R_a \) is restricted by references

Additional constraints:

**dbsm1:**
- **insert:** \( R_a \rightarrow R_{b1} \)
- **delete:** (1) \( R_b \rightarrow (R_{b1}, (R_b)) \)

**dbsm2:**
- **insert:** (1) \( R_b \rightarrow (R_{b1}, R_{b}, R_{ab}, R_{b1}) \)

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5.3.4. Integration with a nest:

(a) NEST AND NEST (figure 13a):

The cardinality of A:B is restricted to 1:1.

**Differences:**

1. In dml (dm2), every \( R_b(R_a) \) tuple must be owned by an \( R_a(R_b) \) tuple.
2. Deletion of an \( R_a(R_b) \) tuple in dml (dm2) requires deletion of the owned \( R_b(R_a) \) tuple.

**Additional constraints:**

- **dbsm1:**
  - insert: \( R_b - (R_b,R_b) \)

- **dbsm2:**
  - insert: \( R_a - (R_a,R_a) \)

Example 14 illustrates this case.
(b) NEST AND PRIMARY (figure 13b):

The cardinality of the relationship \( A:B \) is \( 1:N \).

Differences:

1. In dm2, deletion of \( R_a \) is restricted by references.
2. In dm2, deletion of \( R_b \) results in deletion of owned \( R_b \) tuples, while in dm2 deletion of \( R_b \) is restricted by references.

Additional constraints:

dbsm1:

- insert: (1) \( R_a \cdot R_a, R_{a1} \), (2) \( R_b \cdot (R_b, R_{b1}) \)
- delete: (1) \( R_b \cdot R_{b1}, (R_b) \)

dbsm2:

- insert: (1) \( R_a \cdot R_a, R_{a1} \), (2) \( R_{ab} \cdot (R_{ab}, R_{b1}) \)
6. RELATIONSHIP TO OTHER MODELS

In this section, we examine some of the similarities between the structural model and other data models.

6.1. The relational model:

In relational model theory, the concepts of functional [Codd72] and multivalued [Fagin77] dependency among attributes are important for normalization of relations and data model design. A functional dependency between two attributes $A_1$ and $A_2$, denoted by $A_1 \rightarrow A_2$, means that for each value of $\text{DOM}(A_1)$, a unique corresponding value of $\text{DOM}(A_2)$ can be determined. Functional dependency between two sets of attributes is defined correspondingly. Attributes of a relation $R$ in Boyce-Codd normal form obey the constraint: if any attribute $A$ in $R$ is functionally dependent on a set of attributes $X$ in $R$, and $A$ is not in the set $X$, then all attributes in $R$ are functionally dependent on $X$.

All relations in the structural model are in Boyce-Codd normal form, and hence obey the above constraint. A functional dependency will also exist between each attribute in a referenced relation, and the ruling part of the referencing relation. Hence, a reference connection from a relation $R$ to another relation $R'[A_1, \ldots, A_i]$ defines $i$ functional dependencies $K(R) \Rightarrow A_j; j = 1, \ldots, i$. This is so because a functional dependency $K(R) \Rightarrow X_r$ will exist in relation $R$, where $X_r$ is the set of referencing attributes in $R$. We will also have the functional dependencies $X_r \Rightarrow A_j; j = 1, \ldots, i$. From the transitivity rule for functional dependencies, it follows that $K(R) \Rightarrow A_j; j = 1, \ldots, i$.

Since the structural model is constructed from relations, a relational query system based on the relational algebra or the relational calculus can be used on the structural model. However, additional capabilities exist in the structural representation to simplify expression of queries by making use of represented connections. For example, consider the structural schema in figure 8a. A query such as "FIND THE WORK LOCATION OF EMPLOYEE NUMBER 5" does not have to be expressed as a join between two relations, since the reference connection specifies the department tuple that corresponds to the tuple representing employee number 5.

In the relational model, one has to specify integrity constraints to maintain tuples in different relations in a consistent state. In the structural models, such constraints may be specified implicitly via connections.

6.2. The hierarchical model:

A hierarchical model can be expressed using relations as record types and ownership connections as hierarchical arcs. Hence, if a structural model is restricted such that only ownership connections are used, and such that all relations are connected together in a tree structure, a hierarchical definition tree would result. The difference in representation is the redundancy created by repetition of the ruling part attribute of the owner relations in the owned relations. However, such redundancy need not be implemented in a hierarchical implementation.

6.3. The network model:

The link set concept of the network model can be represented in the structural model. An automatic set can be defined using an ownership connection. Again, the only difference is the redundant representation of the ruling part attributes from the owner relation in the owned relation.
However, the existence of the connecting attributes implicitly specifies the set occurrence when a new member tuple is inserted in the data model without requiring an additional procedure to specify the correct owner.

A manual set can be represented by a 1:N association between two relations, as in the example of figure 8d. Here, the DEPARTMENTS relation corresponds to the owner type, and the EMPLOYEES relation to the member type. Employee tuples can exist without belonging to any department tuple, and the set of members of each department owner tuple is specified via the association.

The implementation oriented features of the hierarchical and network models are implementation dependent, and hence are best left to the implementation phase. We note that the structural model may represent structures that are not part of any of the three other models, as shown in section 4.2.
7. THE DATABASE DESIGN PROCESS

This section summarizes the process of designing the database with the aid of the structural model, and provides a brief discussion of considerations for model implementation. The approach, which we only outline here, provides much of the motivation for concepts presented in the structural model. A detailed description and analysis of the remaining steps of the database design process will be the subject of a later report.

An overview of the entire design process for an integrated database system is given in figure 14. We define three groups of people that participate in the design process: the potential users, the integrators, and the implementors. These groups will interact during the database design process. The vertical axis in figure 14 defines the activities of each group relative to a time frame.

A potential user is a group of people or application programs that expect to use the database system. Many such potential users will exist since we are designing a large, integrated database. Each potential user must analyze his requirements, and define a data model with expected load estimates. Since a database typically serves many diverse but potentially related interests, many such data models can be established.

In section 4.1, we showed how the structural model guides the design of data models. Additional information is solicited from the potential user about his expected use of his data model. This information is not part of the data model, but is attached to the relations and connections of his data model. This includes additional integrity constraints, and expected retrieval and update characteristics for the data model. Load estimates will be classified into several update and retrieval components on the relations and connections of the data model.

The database integrators then undertake to combine these data models into an integrated database model. In the process of combining the data models, conflicts may arise which have to be resolved by changing some of the data models. There may be data models which turn out to be unrelated, or weakly related, to the core of the integrated database model so that they are not included. The result of the data model integration is to define preliminary database submodels for the user groups. This process will need consultation with the users if their data model has to be changed.

The integrators then combine the load estimates from the individual user data models and produce load estimates for the database model. When the transformation from data models to database model is simple, the load estimates can simply be added together. In complex situations, load data will have to be transformed to correspond to the transformation from the data models to the database model.

The implementors then use the cumulative load estimates on relations and connections to design the file structures and access methods. They take into account the expected update and retrieval load of the database model. Connections that are expected to be used frequently should be explicitly represented in the implementation. A methodology for designing the file structures and access methods based on the expected update and retrieval characteristics of relations and connections will be described in a later report.

When usage patterns change, it is reasonable to change implemented file structures and access methods without affecting the structural database model. Only the performance of retrieval and updates along model relations and connections whose implementation is changed will be affected. Provisions should be made in the implementation for such a restructuring.

Provisions must also be made for changing user data models, or for deletion of existing submodels and addition of new data models. This may cause a change in the database model. Structural model changes which only affect rarely used connections will be easier to accommodate than changes which affect very critical and tightly bound connections.
Figure 14. The integrated database design process

We will address the issue of database design and implementation using the structural model in a separate report. We will give a quantitative approach to database design, and discuss possible implementation choices for the structural model constructs.
8. Conclusions:

The model we have presented provides a bridge between the simplicity of the relational model and the explicitness of the network model. On the one hand, all structures in the model are relations in Boyce-Codd normal form that the uniformity of the relational model is maintained. Query techniques devised for relational models can be easily incorporated into the structural model. On the other hand, important structural information about the real-world situation is incorporated in the data model, and provides important knowledge both for potential users and for database system implementors.

We then showed how the different representations in two data models can be integrated, leading to the construction of an integrated database model which correctly supports the different data models of the users. The integrated database model then supports the user submodels.

Our point of view of the implementation process is that connections between relations have to be carefully considered. Binding of important connections will cause reasonable levels of performance to be achieved. At the same time, unbound connections remain recognized, and may be employed when restructuring due to changing demands becomes necessary. The decision of which connections to bind is best supported by inclusion of connections which are candidates for binding in the database model.
References:


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