SOFTWARE RESTYLING IN GRAPHICS AND PROGRAMMING LANGUAGES

by

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ABSTRACT. The value of large software products can be cheaply increased by adding restyled interfaces that attract new users. As examples of this approach, a set of graphics primitives and a language precompiler for scientific computation are described. These two systems include a general user-defined coordinate system instead of numerous system settings, indentation to specify block structure, a modified indexing convention for array parameters, a syntax for n-and-a-half-times-round loops, and engineering format for real constants: most of all, they strive to be as small as possible.

9.3 PHILOSOPHY. Kernighan and Plauger [1976] describe explicitly and by example three precepts of the Software Tools philosophy:
- trim out the inessentials
- build it adaptively
- let someone else do the hard part

Two more examples, driven by the same philosophy, are given below. The basic idea is to obtain high leverage by taking an existing, powerful piece of software and make it useful to more people by designing a new interface. Webster's calls this process facelifting: "a restyling intended to increase comfort or salability."

1.0 JUSTIFICATION FOR STILL ANOTHER PROGRAMMING LANGUAGE. Fortran will no doubt remain for many years the most important programming language for scientific computation. When used carefully and with discipline, it yields remarkably portable codes; this is its greatest virtue. But, as programmers have complained for years, it also has many faults:
- awkward syntax for statements, strings, names
- primitive control structures
- DO loop restrictions
- no macros

Fortran preprocessors, such as MOPTRAN [Cock+Shustek 1975], have eliminated many of these disadvantages and therefore have become very popular. Unfortunately, they reduce portability somewhat, since either the preprocessor must be installed at the new site
or illegible 'object' Fortran sent there. More importantly, such preprocessors have only a minor effect on inherent problems of Fortran:

- dynamic allocation is either unavailable or requires the use of rather confusing tricks
- no PROCEDURE VARIABLE type
- no STRUCTURE type
  (Labelled common blocks, since they do not use the combinatorial possibilities of procedure parameterization, are less flexible.)
- no 0-origin indexing
- array bound information is not automatically passed
- no vector operations
- no recursion

The PCRT library makes dynamic allocation one of its most advertised features: "We have found that use of dynamic storage allocation in PORT leads to more clearly structured programs, cleaner calling sequences, improved memory utilization, and better error detection." [Fox+Hall+Schryer 1977] Adding a stack tc Fortran is a messy affair, however, as shown in figure 1, which contains two alternate methods in FCFT for allocating an

```
SUBROUTINE LBB(A,N)

COMMON /CSTAK/DSTAK(500)

DOUBLE PRECISION DSTAK
INTEGER ISTAK(1000)
REAL A(I)
REAL RSTAK(1000)

EQUIVALENCE (DSTAK(I),ISTAK(I))
EQUIVALENCE (DSTAK(I),RSTAK(I))

II = ISTKGT(2*N,2)
IR = ISTKGT(N,3)

; code referring to RSTAK(IR+n) and ISTAK(II+m)
; probably ending with code to store the stuff
; from the real scratch storage into array A

CALL ISTKRL(2)
RETURN
END

SUBROUTINE LBB(A,N)

COMMON /CSTAK/DSTAK(500)

DOUBLE PRECISION DSTAK
INTEGER ISTACK(1000)
REAL A(I)
REAL RSTAK(1000)

EQUIVALENCE (DSTAK(I),ISTACK(I))
EQUIVALENCE (DSTAK(I),RSTAK(I))

II = ISTKGT(2*N,2)
IR = ISTKGT(N,3)

CALL LIBB(A,ISTACK(II),RSTAK(IR),N)
CALL ISTKRL(2)
RETURN
END
```

figure 1
INTEGER and REAL array.

Other proposals are even more complicated. (After a 7 page description of DYNOSCP, Huybrechts[1977] states: "This paper gives only the basic features of the DYNOSCP system. A more sophisticated use allows the user, once he is familiarized with the system, to improve greatly the speed of programs using it."

PL/I, which is now becoming fairly widely available in some form, overcomes all these difficulties. However, so huge a language tends to overwhelm people, and because of tricky precision rules, silent type conversions (as in I=J=0;), and the like, learning only part of the language is dangerous.

Other languages, while beautifully designed, have their own flaws. For example, Algol W does not have a robust interface to Fortran; in addition to this [Nohilner 1977], Pascal places painful restrictions on arrays.

1.1 T. Thus another approach seems warranted, which can combine the needed features of PL/I, the deliberate syntax of ALGOL, and the low implementation cost of the Fortran preprocessors. such an approach has produced the language T, intended to assist in the implementation and documentation of algorithms for scientific computation. The principal aims have been ease of reading and writing, low implementation cost, and reasonable efficiency.

Appendix T gives the formal language proposal, specifying the syntax according to Wirth's proposal [1977]. Since T is similar to Fortran, Algol 60, and PL/I, a complete specification of the semantics may be omitted without confusion. To provide the heuristics behind the design choices and to give an overview of the language, various aspects of the following example will be discussed.

TRIP EAR

# example of T and G systems:
# various views of the sum of three Gaussian peaks:
# Eric Grosse  Stanford University

REAL: AZIM, ELEV, # VIEWING ANGLES FOR SURFACE PLOT
   RELERF, ABSEPR, # ERROR TOLERANCES FOR ODE
   T, TOUT, # INDEPENDENT VARIABLES OF TRAJECTORY
   NORMYP

REAL (2) : LL, UR, # CORNERS OF RECTANGULAR DOMAIN OF FUNCTION
   ORIGIN, # FOCAL POINT FOR SURFACE PLOT
   X0, SCALE, # COORDINATE TRANSFORMATION PARAMETERS
   Y, YP # LOCATION AND GRADIENT FOR TRAJECTORY

REAL (142) : ODEWORK

INTEGER (5) : ODEIWORK
DEFINE(P,20)     # density of P samples;
REAL(-P:<P,-P: I?): P TABLE
REAL(3): LEVEL    # CONTOUR LEVELS
INTEGER: I, J,
IFLAG          # DIAGNOSTICS FLAG FOR ODE
STRUCTURE: PAPA?! # LOCATIONS, HEIGHTS, AND WIDTHS OF PEAKS
REAL(3): X
REAL(3): H, W  # PLOT PILE
STRUCTURE: PP

INTEGER(500): WORK
PROCEDURE: GOPEN, GCLOSE, GPICT, GCONT, GSURF, GL TYPE,
GJUMP, GDRAW, GTRAN
FORTRAN PROCEDURE: CDE, DF, STASH
PROCEDURE () REAL: F

# SET UP PARAMETERS
BLANK SEPARATION (2)
REAL DIGITS(3)
GET DATA(AZIM,ELEV)
PUT DATA(AZIM,ELEV)
X(1,1) := 0
X(1,2) := 0.5
X(2,1) := -0.43'301 2702
X(2,2) := -0.25
X(3,1) := -X(2,1)
X(3,2) := X(2,2)
PUT DATA ARRAY(X)
GET ARRAY(H)
PUT DATA ARRAY(H)
GET ARRAY (W)
PUT DATA ARRAY(U)
STASH(X,H,W)
FOR ( -P <= I <= P )
   Y(1) := FLOAT(I) / P
   FOR ( -P <= J <= P )
      Y(2) := FLOAT(J) / P
      P TABLE(I,J) := P(Y,PARAM)

# SURFACE PICT
GOPEN('VEP12FP',PF)
GPICT(PF)
LL := -1
UR := 1
ORIGIN := 0.5
GSURF(LL,UR,FTABLE,AZIM,ELEV,ORIGIN,0.25,PF)
* CONTOUR PLOT

GPICT(PP)
SCALE := 0.3333
X0 := -0.5/SCALE(1)
GTRAN1(X0,SCALE,PP)
GET AARRAY (LEVEL)
PUT DATA AARRAY(LEVEL)
GCONT(UL,UR,PTABLE,LEVEL,PP)
GLTYPE('DOT',PP)
GET AARRAY(LEVEL)
PUT DATA AARRAY(LEVEL)
GCONT(UL,UR,PTABLE,LEVEL,PP)

* COMPUTE AND PLOT TRAJECTORY

RELELB := 10(-6)
GLTYPE('SOLID',PP)
ABSE3R := 10(-6)
WHILE ( NOT END OF INPUT )
GET AARRAY ( Y )
PUT DATA AARRAY( Y )
T := 0
GJUMP(Y,PP)
IFLAG := 1
WHILE( NORMYP > 1(-3) & 1<=IFLAG & IFLAG<=3)
TOUT := T + 10(-3)/NORMYP
CDE (DP, Z, Y, T, TOUT, RELERR, ABSERR, IFLAG, ODEWORK, ODEIWORK)
CASE
2 = IFLAG
GDRAU(Y,PP)
3 = IFLAG
PUT('ODE DECIDED ERRORS TOLERANCES WERE TOO SHALL.')
PUT('NEW VALUES:')
PUT DATA(RELERR,ABSERR)
ELSE
PUT('ODE RETURNED THE ERRCR Flag:')
PUT DATA(IFLAG)
FIRST
DF(T, Y, YP)
NORMYP := NORM2 (YP)
GCLOSE(PP)

F ( Y, PARAM ) Z
REAL(): Y
REAL: Z, NORMSQ
STRUCTURE: PARAM
REAL(3,2): X
REAL(3): H, W
INTEGER: I
Z := 0
FOR ( 1 <= I <= 3)
NORMSQ := (Y(1)-X(I,1))^2 + (Y(2)-X(I,2))^2
Z := Z + H(I)*EXP(-0.5*W(I)*NORMSQ)
1.2 CONTROL AND OTHER SYNTAX. Perhaps the most striking feature the Algol veteran sees in this example is the complete absence of BEGINs and ENDs. Not only is the text indented, but the indentation actually specifies the block structure of the program, Such a scheme was apparently first proposed by Landin [1966]. Except for an endorsement by Knuth [1974], the idea seems to have been largely ignored.

Ideally, the text editor would recognize tree-structured programs [Hansen 1971]. In practice, text editors tend to be line oriented so that moving lines about in an indented program requires cumbersome manipulation of leading blanks. Therefore the current implementation of T uses BEGIN and END lines, translating to indentation on output. Thus the input

```
STRUCTURE: PARAM
  (( REAL(3,2) : X
    REAL(3) : H, W
  ))
```

produces the output

```
STRUCTURE: PARAM
  REAL (3,2) : X
  REAL (3) : H, W
```

Whatever the implementation, the key idea is to force the block structure and the indentation to be automatically the same, and to reduce clutter from redundant keywords.

Blanks are insignificant outside of strings. Mathematical tables have long used blanks inside numeric constants, as in

```
PI := 3.14159 26535 89793
```

for readability. Blanks in identifiers also can improve readability, while reducing the chance of misspelling and easing the pain of name length restrictions imposed by the local operating system.

In accordance with the recommendations of Scowen+Wichmann [1973], comments start with a special character, #, and run to the end of the physical line.

The small reserved word list eliminates the need for a stringing convention. The psychological advantages of this approach have been elaborated by Hansen [1973].

The form of the assignment and procedure call statements follows the clean, clear style of Algol 6C. To make macros more understandable, their syntax and semantics match those of procedures as closely as possible.

In addition to normal statement sequencing and procedure calls, three control structures are provided. The CASE and WHILE statements are illustrated in this typical program segment:
WHILE( NORMYP > 1(-3) & 1<=IFLAG & IFLAG<=3 )
   TOUT := T + 10(-3)/NORMYP
   ODE (DF, 2, Y, T, TOUT, RELERR, ABSERR, IFLAG, ODEWORK, ODEIWORK)
   CASE
     2 = IFLAG
     GDRAW (Y, PP)
     3 = IFLAG
     PUT ('ODE DECIDED ERROR TOLERANCES WERE TOO SMALL.')
     PUT ('NEW VALUES:')
     PUT DATA (RELERR, ABSERR)
   ELSE
     PUT ('ODE RETURNED THE ERROR FLAG:')
     PUT DATA (IFLAG)
   FIRST
   DF (T, Y, YP)
   NORMYP := NORM2(YP)

The CASE statement is modelled after the conditional expression of LISP: the boolean expressions are evaluated in sequence until one evaluates to YES, or until ELSE is encountered. The use of indentation makes it easy to visually find the relevant boolean expression and the end of the statement.

One unusual feature of the WHILE loops is the optional FIRST marker, which specifies where the loop is to be entered. In the example above, the norm of the gradient, NORMYP, is computed before the loop test is evaluated. Thus the loop condition, which often provides a valuable hint about the loop invariant, appears prominently at the top of the loop, and yet the common n-and-a-half-times-around loop can still be easily expressed.

The FOR statement adheres as closely as practical to common mathematical practice.

FOR ( 1 <= I <= 3 )
   NORMSQ := (Y(I)-X(I,1))**2 + (Y(2)-X(I,2))**2
   Z := Z + H(I) * EXP(-0.5*W(I) * NORMSQ)

Several years experience with these control constructs has demonstrated them to be adequately efficient and much easier to maintain than the alternatives.

Procedure nesting is not used for two reasons. First, textual nesting that extends over many pages is difficult for a human to keep track of. Second, programs typically contain several high level procedures calling a single primitive, so a tree representation is inappropriate anyway.

By removing the nesting of procedures, however, we worsen the problem of entry point hiding that arises when combining programs from many sources into a single library. A solution to this problem is to have an official name for each procedure, coded along the lines of IMSL, and also a more mnemonic nick name (which users can pick for themselves if they like). The macro
processor which is **built** into T can then be used to **change** all occurrences of the nick names into the **corresponding** official names.

1.3 DECLARATIONS. The fundamental scalar types are **INTEGER**, **REAL**, and **COMPLEX**, from which arrays and structures may be **bult** up. As the example

```
REAL (-P:P , -P:P)
```

illustrates, general upper and lower bounds are **allowed**.

The upper bound expression is omitted for a formal array parameter, so that an appropriate value can be taken from the length of the corresponding actual array argument. The **origin** of an actual array argument need not match the origin of the corresponding formal array parameter. For example, if the actual argument A was declared **REAL(0:7): A** and the formal parameter B was declared **REAL(:): B**, then B(8) will correspond to A(7). Host languages, when they allow lower bounds at all, do not permit this flexibility, which is used in the example program when a matrix with lower bound **-P** is passed to a general purpose library routine which assumes a lower bound of **0**.

Structures of arbitrary depth may be declared. As the examples

```
STRUCTURE: PARAM
REAL(3,2): X
REAL(3): H, W
STRUCTURE: PF
INTEGER(500): WORK
```

suggest, structures are useful passing collections of related data, without the need for long parameter lists. This makes feasible the prohibition of global variables in a drastic attempt to **narrow** and make more explicit the interface between procedures. Euclid [Popek+others 1977] has emphasized the importance of visibility of names.

The graphics **procedures** which use the **WORK** vector of the example are able to divide up the space into convenient units. This **capability**, which would be possible in **PL/I** only through the use of pointers, encourages information hiding and abstraction.

**PROCEDURE VARIABLES** allow the names of procedures to be **saved**, an essential feature for applications like the user-specified coordinate transformation described in the graphics syste below.

The importance of existing **Fortran** software is recognized by **providing** for **FORTRAN PROCEDURES** as an integral part of the language. The current **implementation** of I performs this linkage in a more efficient way than the naive user of **PL/I** would be likely to discover,
A novel syntax is introduced for function returns. Since procedures may be recursive, Fortran's convention of using the function name as variable cannot be followed. Instead, the procedure header declares a return variable just like any other parameter:

\[
\text{F (Y, PARAM) Z REAL(); Y REAL; Z}
\]

\[...
\]

1.4 INPUT/OUTPUT. Beginners often find Fortran's input/output the most difficult part of the language, and even seasoned programmers are tempted to just print unlabelled numbers, often to more digits than justified by the problem, because formatting is so tedious. PL/I's list and data directed I/O is so much easier to use that it was wholeheartedly adopted in T. By providing procedures for modifying the number of decimal places and the number of separating blanks to be output, no edit-directed I/O is needed. Special statements are provided for array I/O so that, unlike PL/I, arrays can be printed in orderly fashion without explicit formatting.

Since almost as much time is spent in scientific computation staring at pages of numbers as at pages of program text, much thought was given to the best format for displaying numbers.

In accordance with the "engineering format" used on Hewlett-Packard calculators and with standard metric practice [GM Service Section 1977], exponents are forced to be multiples of 3. As figure 2, an excerpt from the example program's output, shows, this convention has a histogramming effect that concentrates the information in the leading digit, as opposed to splitting it between the leading digit and the exponent, which are often separated by 14 columns. The use of parentheses to surround the exponent, like the legality of imbedded blanks, was suggested by mathematical tables. This notation separates the exponent from the mantissa more distinctly than the usual E format.

1.5 DISCUSSION.

Following Kernighan+Plauger [1976], the initial implementation is unsophisticated [Comer 1978]. Nevertheless, the preprocessing is less costly than the PL/I compile, so the overall results are quite satisfactory. (The evaluation looks even better if one compares PL/I + T against PL/I + PL/I's macro preprocessor.) Most of the processor cost lies in basic I/O; by integrating the macro processor with the language translator, this cost has been minimized. [Kantorovitz 1976] Much of the two-man-months spent in implementation were spent in understanding nooks and crannies of PL/I.
<table>
<thead>
<tr>
<th>Value</th>
<th>Format</th>
</tr>
</thead>
<tbody>
<tr>
<td>53.5106</td>
<td>(-03)</td>
</tr>
<tr>
<td>51.3109</td>
<td>(-03)</td>
</tr>
<tr>
<td>46.7211</td>
<td>(-03)</td>
</tr>
<tr>
<td>40.6514</td>
<td>(-03)</td>
</tr>
<tr>
<td>33.7036</td>
<td>(-03)</td>
</tr>
<tr>
<td>26.4900</td>
<td>(-03)</td>
</tr>
<tr>
<td>10.9000</td>
<td>(-03)</td>
</tr>
<tr>
<td>11.3401</td>
<td>(-03)</td>
</tr>
<tr>
<td>3.63506</td>
<td>(-03)</td>
</tr>
<tr>
<td>-4.12944</td>
<td>(-03)</td>
</tr>
<tr>
<td>-11.9123</td>
<td>(-03)</td>
</tr>
<tr>
<td>-19.7092</td>
<td>(-03)</td>
</tr>
<tr>
<td>-27.5246</td>
<td>(-03)</td>
</tr>
<tr>
<td>-35.3243</td>
<td>(-03)</td>
</tr>
<tr>
<td>-43.1176</td>
<td>(-03)</td>
</tr>
<tr>
<td>-50.9060</td>
<td>(-03)</td>
</tr>
<tr>
<td>-60.6041</td>
<td>(-03)</td>
</tr>
<tr>
<td>-74.1973</td>
<td>(-03)</td>
</tr>
<tr>
<td>-61.9297</td>
<td>(-03)</td>
</tr>
<tr>
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<td>(-03)</td>
</tr>
<tr>
<td>-105.010</td>
<td>(-03)</td>
</tr>
<tr>
<td>-112.670</td>
<td>(-03)</td>
</tr>
<tr>
<td>-120.302</td>
<td>(-03)</td>
</tr>
<tr>
<td>-127.910</td>
<td>(-03)</td>
</tr>
<tr>
<td>-135.493</td>
<td>(-03)</td>
</tr>
<tr>
<td>-143.050</td>
<td>(-03)</td>
</tr>
</tbody>
</table>

Figure 2

T is not intended to replace any existing languages. For distributing mathematical software, Fortran remains the only practical medium; for character processing, something like PL/I or SNOSOL should be used. Still, for the bulk of scientific computation, Fortran should be the easiest to use, particularly since it coexists comfortably with Fortran and PL/I. On the other hand, one can imagine ways that T right be improved, as well.

Features omitted for ease of implementation include:
- trimmed arrays, like `X(2:N)`
- procedure results of general type
- conditional boolean operators that do not evaluate their arguments when it is possible to avoid doing so
- a swap operator

For other features, no entirely satisfying design was apparent:
- strings
- more general procedure calls (such as indefinite number and type of arguments)
- a means of constructing arrays directly from components, as
a string constant constructs a string from individual characters - a means of specifying the invocation graph of who calls whom.

Perhaps the most fundamental though unavoidable flaw is that, unlike LISP, the language is not trivial, and therefore programs cannot be trivially manipulated.

2.0 JUSTIFICATION FOR STILL ANOTHER SET OF GRAPHICS PRIMITIVES.
The next example of restyling is a simple but reasonably complete interface for noninteractive device-independent graphics. In addition to the basic line drawing primitives, higher level procedures are provided for displaying functions of one or two variables. This interface has been implemented as a library of PL/I procedures which call the SLAC Unified Graphics package written by Robert Reach [1978].

Unified Graphics, with its emphasis on the ability to drive displays like the IBM 2250, is troublesome to use directly for function plots and the like. In contrast, Top Drawer, another graphics system at SLAC, allows for function plots but little else. The collection described in detail in Appendix G is meant to strike a useful balance between these two extremes, and contains most of the features of DISPLIA important for scientific computation.

2.1 ESTABLISHING THE ENVIRONMENT. The following excerpt from the example program given in section 1.1 above illustrates typical preparation for plotting:

```
STRUCTURE: P F # PLOT FILE
   INTEGER(500): WORK
   REAL(2): LL, UB, ORIGIN,
            X0, SCALE
GOOPEN('VEP12FP',PP)
GPICT(PP)
SCALE := 0.3333
X0 := -0.5/SCALE(1)
STRA(N(X0,SCALE,PP)
```

The plot area PF is used to remember various options and to buffer low level plotter instructions. This work area is initialized by the GOOPEN call, which specifies the output device. (In the current implementation, no corresponding JCL changes are necessary.) The ease with which devices may be changed is very useful in tuning a plot for publication.

For compatibility with numerical procedures, REAL variables are in full precision, not short. At the start of each new picture, which might be a screenful on a CRT or an 8.5 by 11" page on an electrostatic plotter, GPICT is called.
All plotting is done relative to a user **coordinate** system, which is specified by calling

\[
\text{GTRAN}(\text{F, PP })
\]

where F is the name of a procedure which, when called in the form

\[
\text{F( X, W, PP )}
\]

\[
\text{REAL(N): X} \quad \text{N}<10
\]

\[
\text{REAL(2): W}
\]

will map the point X in user coordinates into a point W in the unit square \([0,1] \times [0,1]\). Normally W(1) is thought of as horizontal and U(2) as vertical. By extending \(\text{PP}\), the user can pass parameters to F. For convenience, the default transformation maps

\[
W := \text{SCALE} \times (X - X0)
\]

2.2 DRAWING, **DIMENSIONING**, AID FUNCTION **GRAPHING**. The basic drawing commands are \(\text{GJUMP, GDRAW, and GTEXT}\) for drawing lines and **adding text**. If a nonlinear coordinate system has been specified, \(\text{GDRAW}\) produces a piecewise linear **approximation** to the implied curve.

A procedure **GGPH** is provided which automatically samples function values, sets up an appropriate scaling, graphs the function, and dimensions the **graph** using **rcund** numbers in a style consistent with the format used by T. Figure 3, taken from Chan [1978], is a typical plot.

The scheme for choosing round numbers is based on the algorithm by Dixon+Kronmal [1965]. Experience and an informal survey of what people would accept as being "**round numbers"** led to various refinements. As in Unified Graphics, the choice is optimized over a reasonable number of **major** tick marks. The total number of tic marks, major and minor, is not allowed to be either too dense or too sparse. For a while, the number of minor tick marks was chosen so that each interval had length \(10^{**k}\), but for input data limits \((200,70)\) the resulting tick marks were at \((-100,0,100,200)\), so this rule had to be relaxed to "either length \(10^{**k}\) or midpoint of major interval? If the difference between the data limits is small compared to the magnitude of the limits themselves (as occurs for example in plotting a nearly constant function), then the labels may become unreasonably large. Special provision is made for this case.

Other routines are available for scatter, surface, and contour plots. The contour computation uses **piecewise** quadratic surface fitting to ensure smooth contours and proper representation of critical points [Marlow+Powell 1976]. Figure 4 presents output from the example **program**, which computes hill-climbing trajectories for a three-gaussian-peak terrain.
Scheme LF2DF2, $E_p = 0.01$

**Figure 3**
CONCLUSION. With a level of effort comparable to writing a Fortran preprocessor, we have created, by compiling into PL/I, a language substantially better than Fortran or its derivatives. Since PL/I problems cannot be altogether avoided by this approach, further work on a language like T could be useful. Perhaps the effort would be better spent on making LISP a practical language for scientific computation by building on the research in symbolic computation.

Like PL/I, Unified Graphics is good for a wide range of applications. But in practice, many people won't use either. For languages, they stick to Fortran; for graphics, they plot by hand or not at all. In both cases it has proven possible to cheaply restyle the existing system, via a preprocessing phase or driver routines, in order to create more agreeable tools.

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